

# LONG-TERM MICROWAVE POWER DRIFT OF A CESIUM FREQUENCY STANDARD AND ITS EFFECT ON OUTPUT FREQUENCY

W. A. Johnson,  
S. K. Karuza, and F. J. Voit  
Electronics Research Laboratory  
The Aerospace Corporation  
P. O. Box 92957  
Los Angeles, CA 90009

## Abstract

*It has been shown previously that the long-term frequency stability of a cesium (Cs) frequency standard is affected by variations in the standard's internal microwave power source [1,2]. Studies were performed on a commercial Cs frequency standard for a period of 20 days, to determine the stability of its microwave power source. The results were then analyzed statistically, and the effects of microwave power drift on the standard's frequency stability were calculated.*

## INTRODUCTION

Studies were performed in our laboratory on cesium (Cs) frequency standards (clocks) made by different manufacturers, to determine the effect of microwave power variations on the output frequency of the standard at different settings of the C-field current. Figure 1 is a block diagram of the test set-up. The results were reported in [3,4]. In one particular Cs frequency standard, we wanted to determine the stability of its own internal microwave power source and the effect of this stability on the frequency stability of the standard.

During the last 20 days of the experiment the zero offset of the microwave power meter was recorded manually. These data were then used to correct the actual measured microwave power values by enabling power meter drift to be eliminated. These results are reported herein. We note that because we have many components in series with the clock electronics, we cannot say that the power variations we measured are completely attributable to the clock itself. It is likely that the resulting power variations are somewhat worse than would be the case for a normal clock configuration.

## MEASUREMENTS

During the 20-day measurement period there were three separated data runs lasting approximately 3, 6, and 10 days. At the beginning of each run the power meter was zeroed. Because we could not zero the meter during a run without stopping the program, we periodically increased the microwave attenuator setting by 60 dB and read the meter's output in microwatts. During the data taking, the power level into the meter was on the order of  $50 \mu\text{W}$ . Sixty dB below this is thus  $50 \times 50^{-6} \mu\text{W}$ , which is very much less than the smallest nonzero power ( $0.01 \mu\text{W}$ ) that the system can read. Thus, increasing the attenuation by 60 dB was equivalent to terminating the meter with a load; indeed, it was probably better, because no microwave connections were changed. The measured power offsets are plotted in Figure 2.

Each of the three data runs consisted of the following steps:

1. Set the C-field at a low value (6 to 8 mA) and the power at the optimum value (i.e., for maximum beam current) of  $-12.5 \text{ dBm}$ .
2. Measure the beat frequency over some long averaging time  $T$ .
3. Increase the power level by 1 dB to  $-11.5 \text{ dBm}$ .
4. Measure the beat frequency over  $T$  again.
5. Increase the C-field current by some prescribed amount (typically 1 mA in our data sequence).
6. Measure the beat frequency over  $T$  again.
7. Change the power back to  $-12.5 \text{ dBm}$ .
8. Measure the beat frequency over  $T$  again.
9. Increase the current again.
10. And so on.

The last C-field current is typically 22 mA.

Each time either the C-field current or the microwave power is changed, there is a waiting period of approximately 5 minutes before data taking begins. This wait ensures that if the clock loop goes out of lock, it will have more than adequate time to relock. For the particular clock measured, the maximum time to acquire relock is about 2 minutes. It is during these 5-minute waits that the power meter's zero offset is read. Figure 2 is a plot of these zero offsets as a function of time. Note that the offsets are all either zero or negative. A negative value for the offset means that all powers measured are actually larger by the amount of the offset.

Figure 3 is a plot versus time of the two measured power levels. The corrected power data were fit with a second-order function, i.e.,  $a_0 + a_1t + a_2t^2$ . Figure 4 is a plot versus time of the high and low power-level fits, and Figure 5 is a plot, versus time, of the difference between the two fits. Figures 6 and 7 are plots of the residuals that are left after the fit curve is subtracted from the corrected power data.

To determine the contribution of the power measurement equipment, the stability of the actual power meter used to obtain the data was measured. Figure 8 is a block diagram of the measurement system. Figures 9 and 10 show the results of two long data runs, one for about 10 days and the other for about 16 days. Each data point is for an averaging time of about 2.8 hr. Note that the standard deviation of each data set is much less than the standard deviations in Figures 6 and 7. The data-point separation in time for Figures 6 and 7 varies, but it is close as 0.14 days (3.36 hr) and this is comparable to that in Figures 9 and 10. The conclusion is that drifts in the power meter, in its calibrator, and in the power measurement head contribute negligibly to the measurements plotted in Figures 6 and 7.

## DATA STATISTICS

Because of the very regular manner in which the data were taken, there occurred systematic time separations in the data of 0.14 and 0.41 days. The data could also be averaged to give results for 0.82 and 2.5 days. These data were then analyzed statistically. The results are summarized in Table I. Column 1 is the time  $\tau$  between measurements. Column 3 is the Allan standard deviation of the power as a function of  $\tau$ . Column 2 is the number of data points used to calculate the results in Column 3. Figure 11 is a plot of the change in clock output frequency for a 1-dB change in microwave power as a function of the C-field setting. The factor  $8 \times 10^{-13}$  comes from Figure 11 and represents about the worst C-field-setting coefficient of frequency change per dB of power change over the Zeeman frequency range 25 to 51.5 kHz. Column 4 is approximately the maximum Allan standard deviation that would be caused by the power changes in column 3. Column 5 has calculated values of  $3.55 \times 10^{-11}/\sqrt{\tau}$ ; this equation is derived from Figure 12, which is a plot of the Allan standard deviation of the Cs clock as measured against our HP-50613-004 standard.

## CONCLUSIONS

One can conclude from the data in Table I, as plotted in Figure 13, that even if the C-field is set far away from an optimum setting, the effect of changes in microwave power on the Allan standard frequency deviation will be small for periods of less than 2.5 days. Even at 2.5 days, the Allan standard frequency deviation that results from beam tube noise is still about twice what would result from microwave power changes in this particular standard. Thus, if the Allan standard deviation of the power remained about constant, the Allan standard frequency deviation due to beam tube noise and that due to microwave power variations would be about equal at 10 days.

## ACKNOWLEDGMENT

The authors thank Mr. Michael Meyer of The Aerospace Corporation for editing and preparing this paper.

## REFERENCES

1. A. De Marchi, "Rabi Pulling and Long-Term Stability in Cesium Beam Frequency Standards," *IEEE Trans. Ultrasonics, Ferroelectrics, and Frequency Control* UFFC-34 (6), 598-601 (November 1987).
2. A. De Marchi, "New Insights into Causes and Cures of Frequency Instabilities (Drift and Long-Term Noise) in Cesium Beam Frequency Standards," *Proc. 41st Frequency Control Symposium, 1987*, pp. 54-58.
3. S. K. Karuza, W. A. Johnson, and F. J. Voit, "Determining the Effects of Microwave Power and C-field Setting on the Frequency of a Cesium Atomic Frequency Standard," *Proc. 3rd European Time and Frequency Forum (Besancon, France, 21-23 March 1989)*, pp. 69-72.

4. S. K. Karuza, W. A. Johnson, J. P. Hurrell, and F. J. Voit, "Determining Optimum C-field Settings that Minimize Output Frequency Variations in Cesium Atomic Frequency Standards," presented at the 21st Annual Precise Time and Time Interval (PTTI) Applications and Planning Meeting, Redondo Beach, Calif., 30 November 1989.

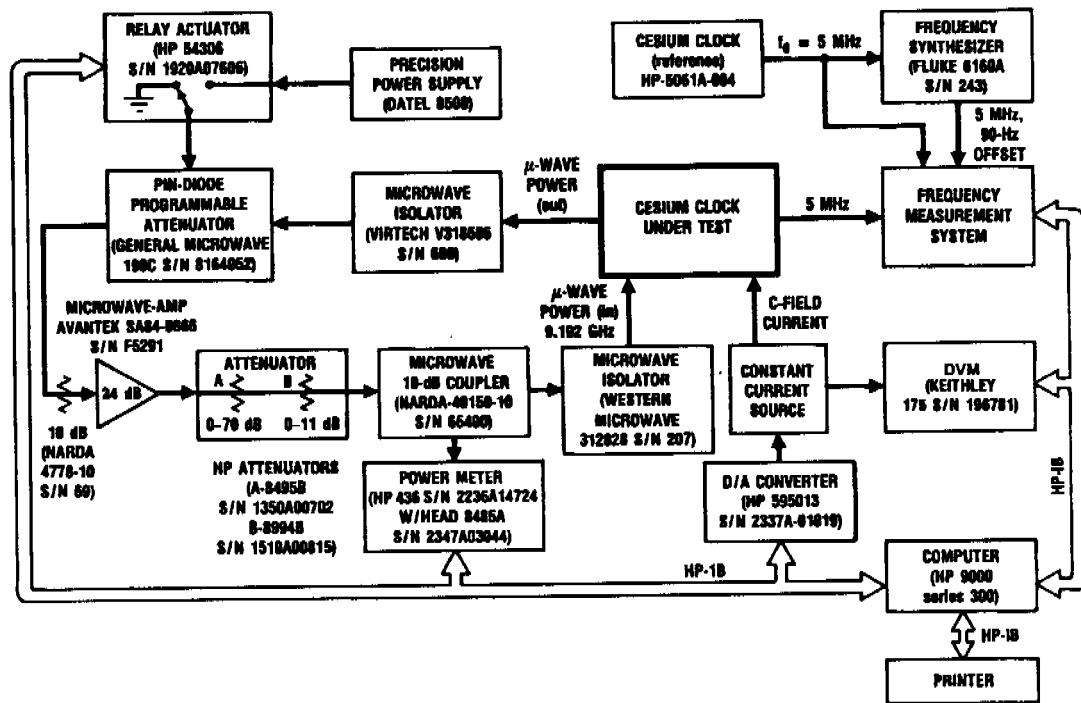


Figure 1. Block Diagram of the C-field Measurement System for a Cs Frequency Standard

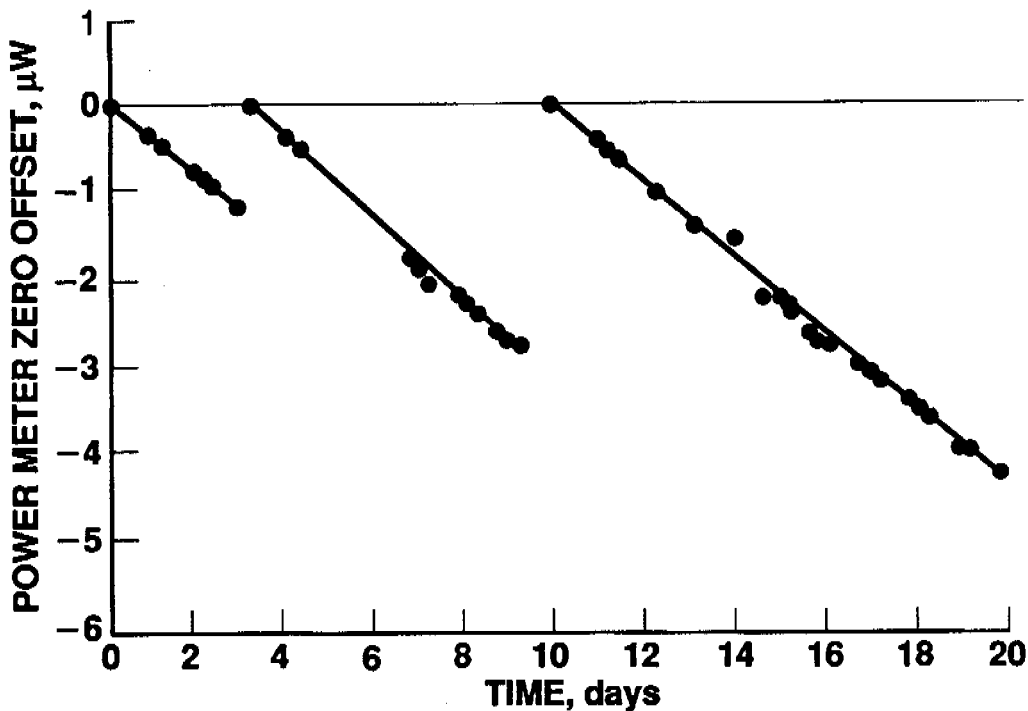


Figure 2. Plot of the Power Meter Zero Offset as a Function of Time

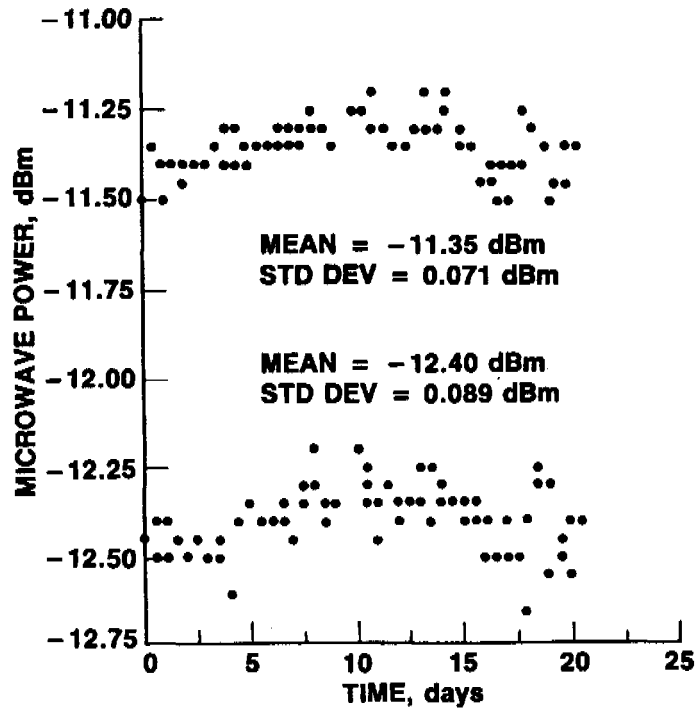


Figure 3. Plot of the Two Measured Power Levels as a Function of Time

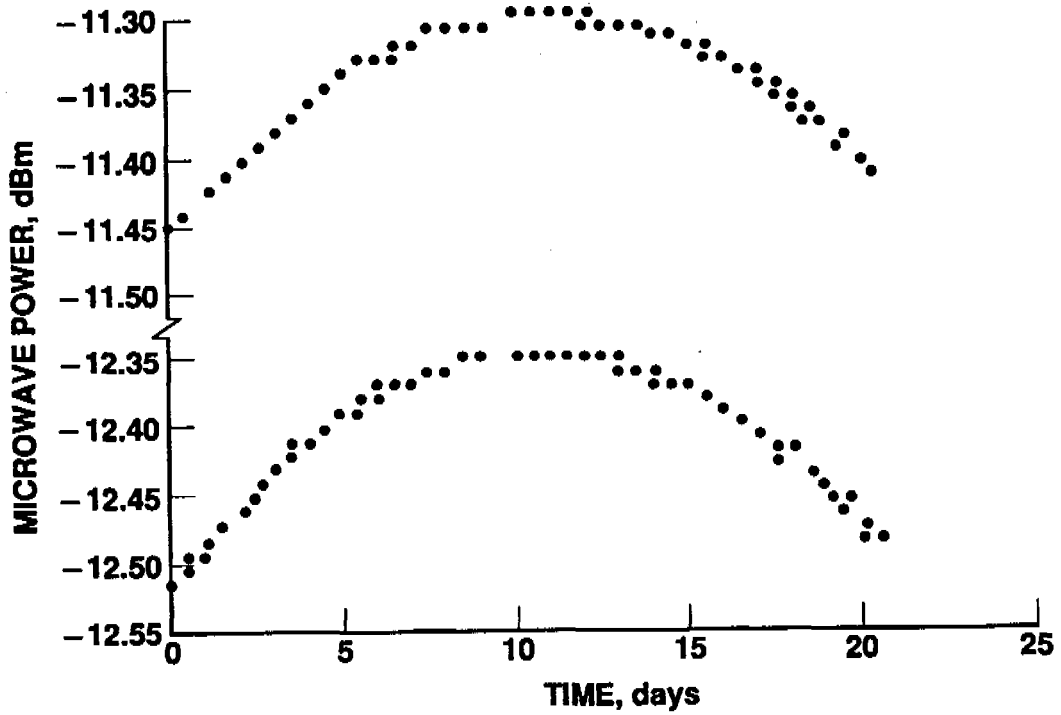


Figure 4. Plot of the Curve Fits of the Two Measured Power Levels as a Function of Time

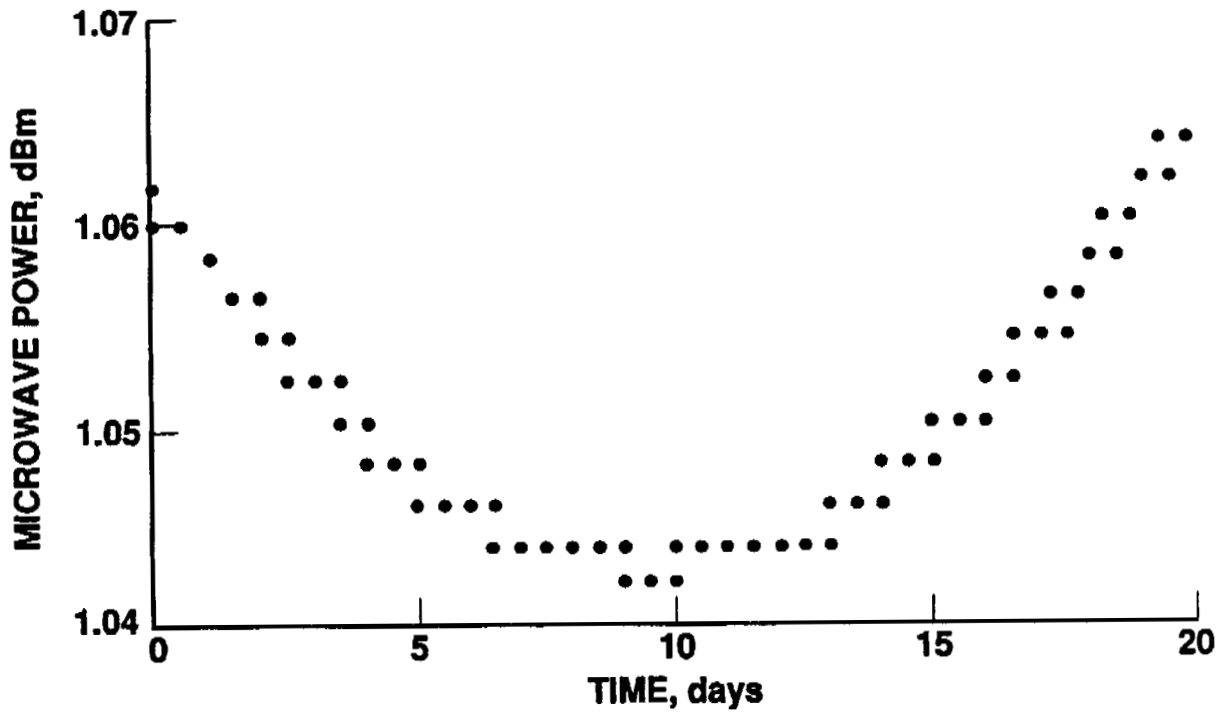


Figure 5. Plot, as Function of Time, of the Difference of the Two Fits to the Power Data

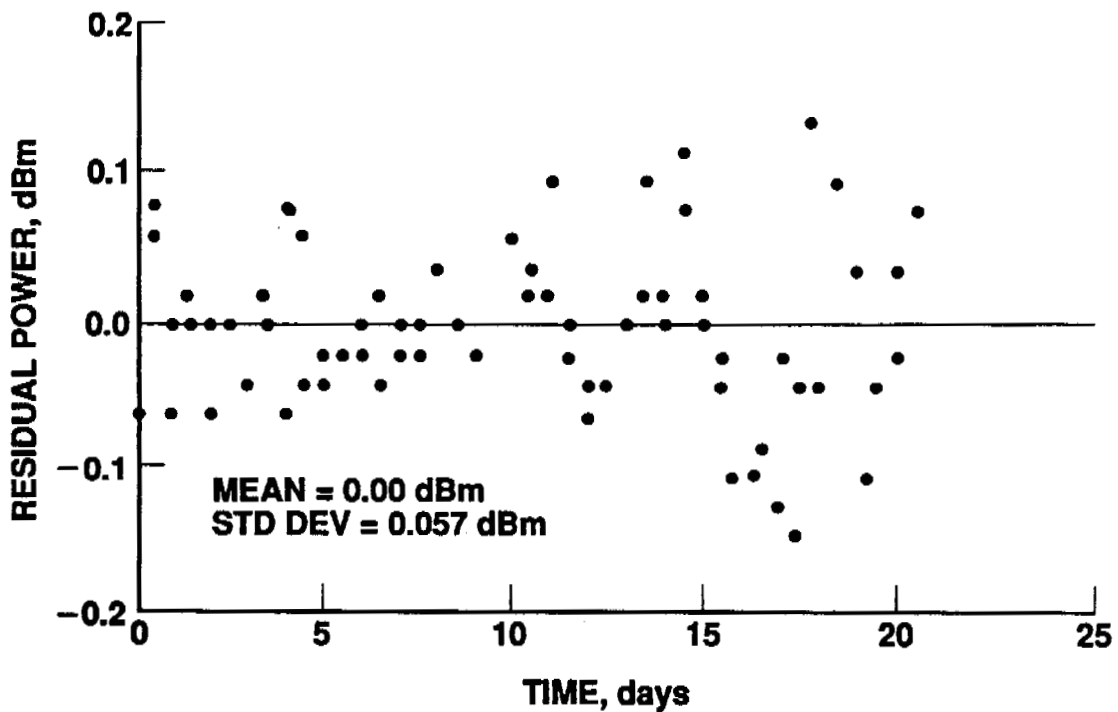


Figure 6. Plot, as a Function of Time, of the High-Power Residuals that Remain after the Fit Curve is Subtracted

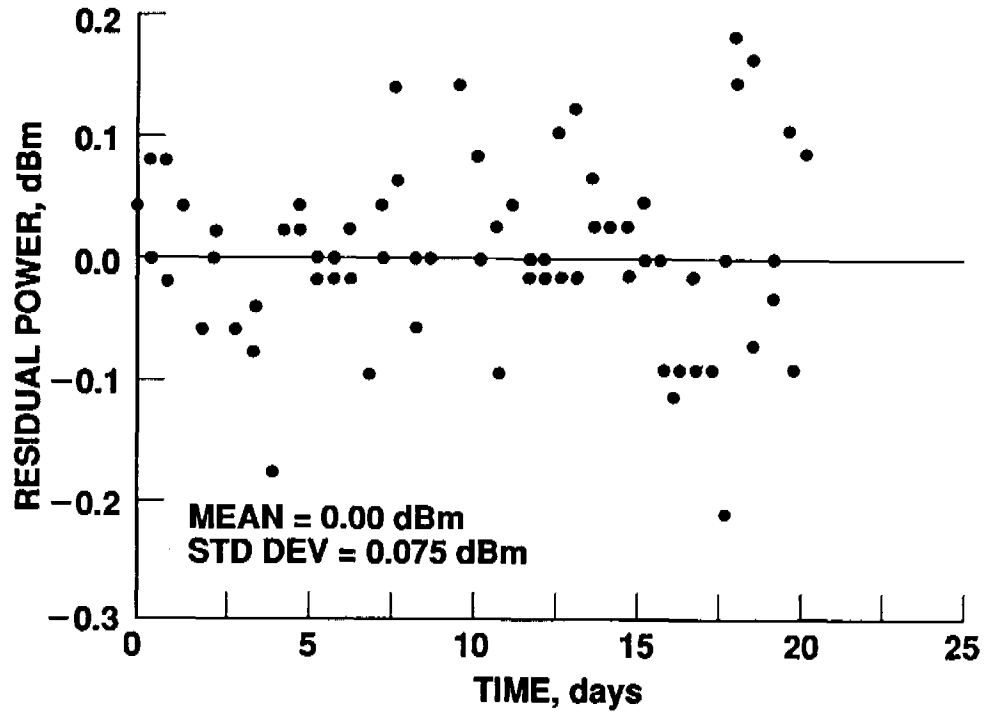


Figure 7. Plot, as a Function of Time, of the Low-Power Residuals that Remain after the Fit Curve is Subtracted

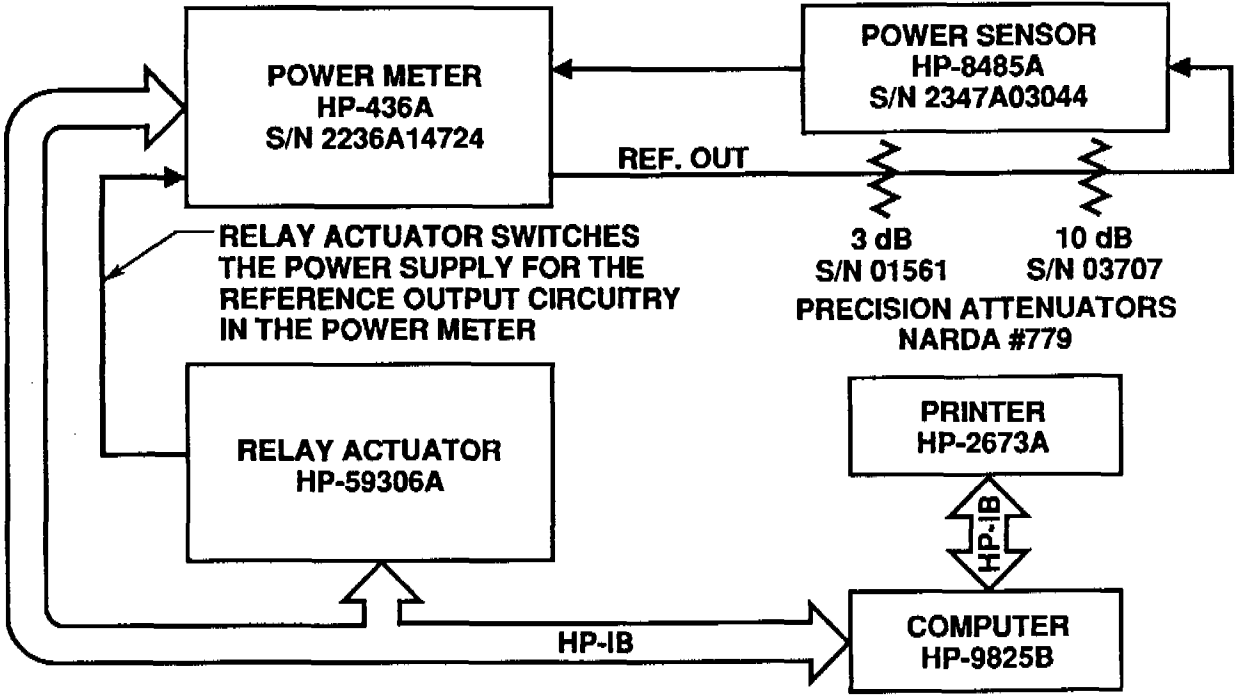


Figure 8. Block Diagram of the Power Meter Measurement System



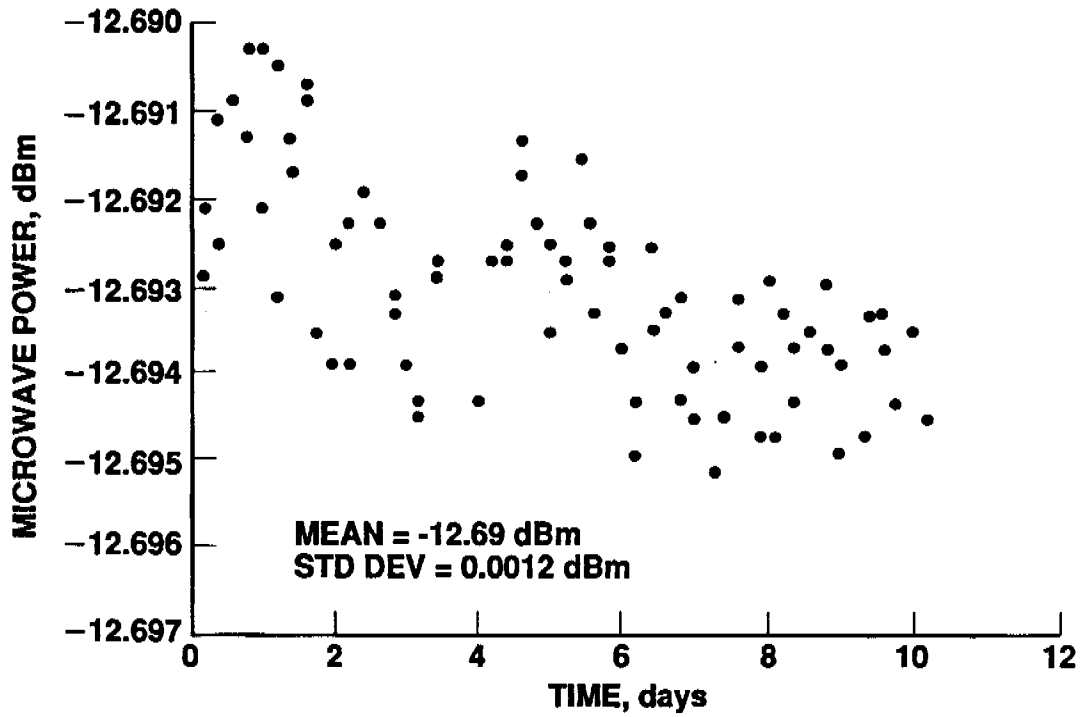


Figure 9. Plot of the Stability of the Power Meter for a 10-Day Run

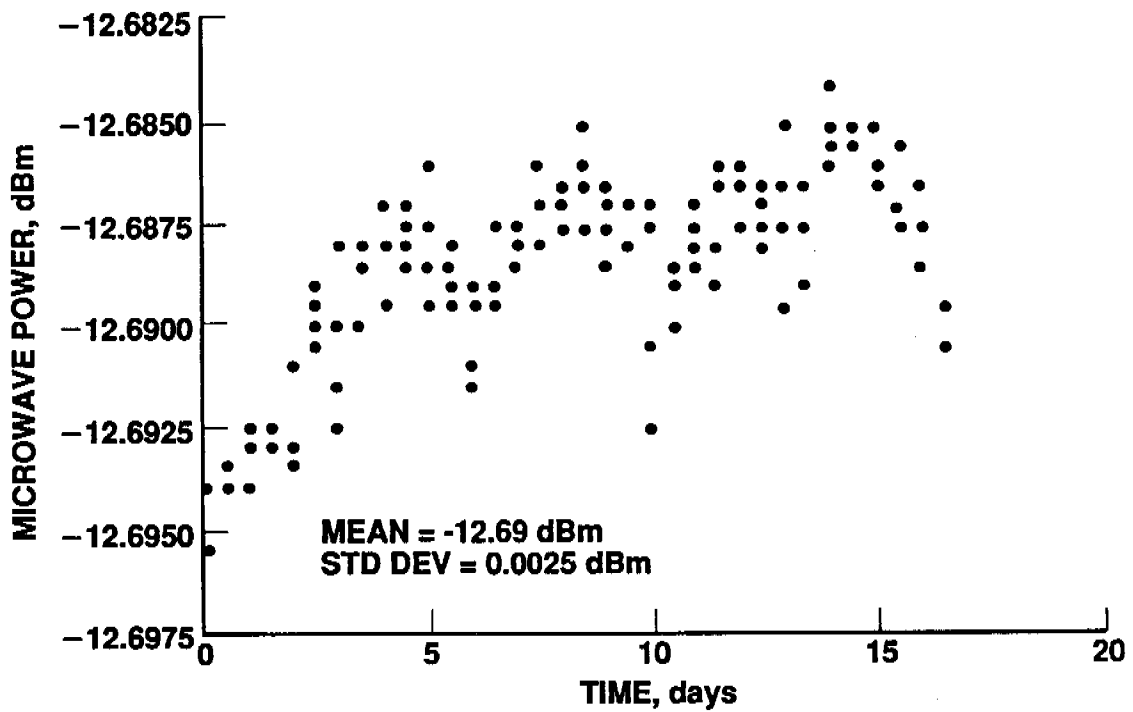


Figure 10. Plot of the Stability of the Power Meter for a 16-Day Run

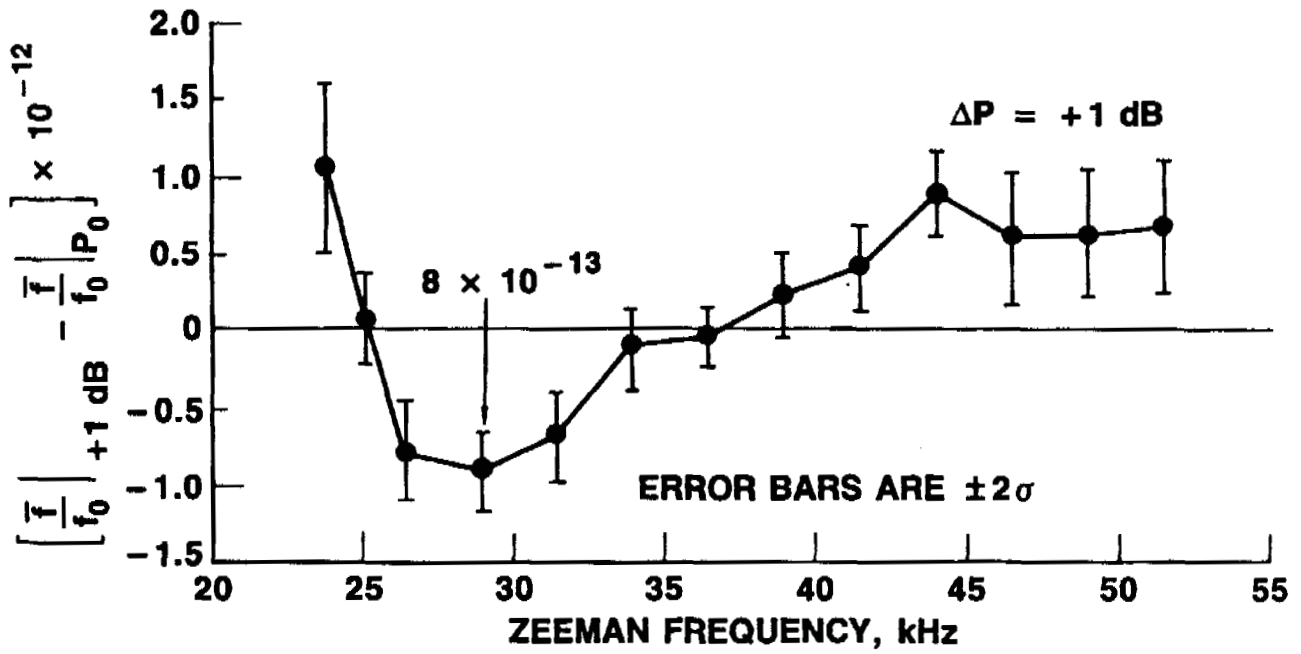


Figure 11. Difference of the Average Frequencies of the Cs Frequency Standard as a Function of C-field for a Microwave Power Change of +1 dB above the Optimum Power Level  $P_0$

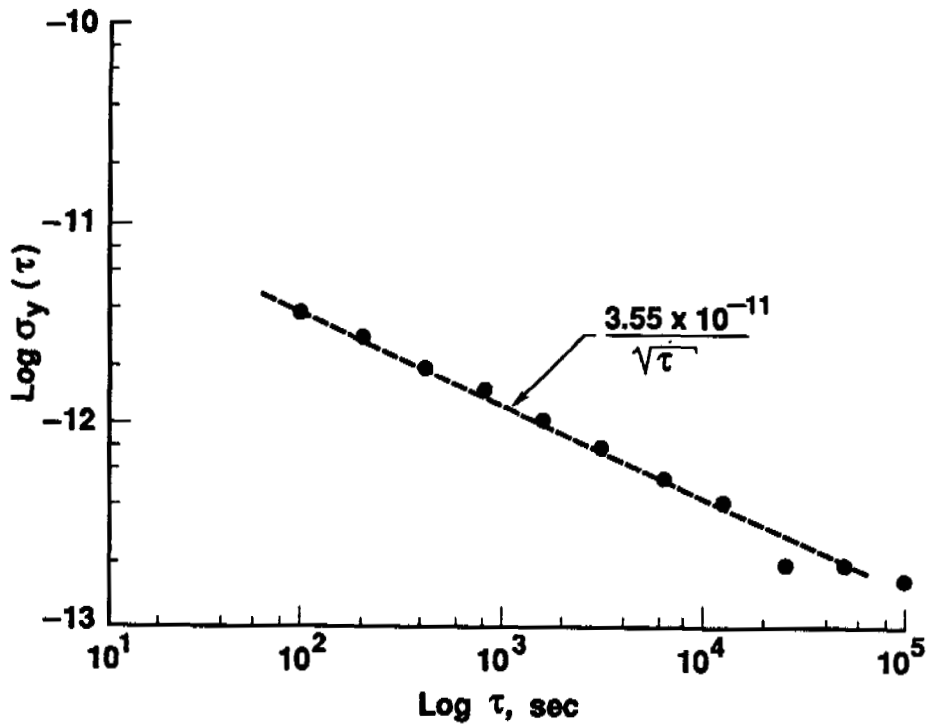


Figure 12. Plot, as a Function of Sampling Time, of the Allan Standard Frequency Deviation of the Cs Frequency Standard

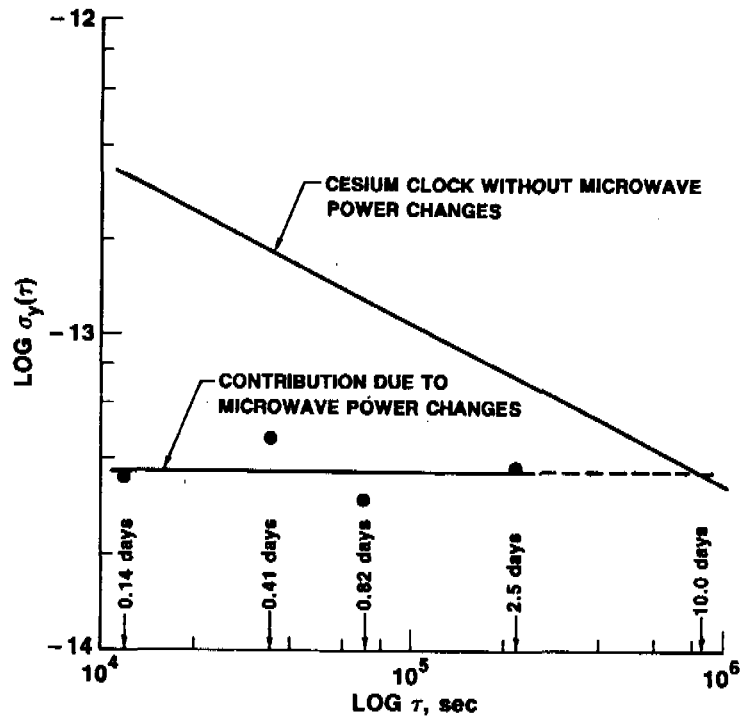


Figure 13. Plot of the Calculated Contribution of Microwave Power Changes to the Allan Standard Frequency Deviation of the Cs Frequency Standard

Table 1. Measurement Data

POWER DATA			FREQUENCY DATA	
TIME ( $\tau$ ), days	No. OF POINTS	ALLAN STD DEV [ $\sigma_p(\tau)$ ], dBm	ALLAN STD DEV [ $\sigma_y(\tau) \approx \sigma_p(\tau) \times 8 \times 10^{-13}$ ]	$\frac{3.55 \times 10^{-11}}{\sqrt{\tau}}$
0.14	128	0.04390	$0.3512 \times 10^{-13}$	$3.228 \times 10^{-13}$
0.41	64	0.05794	$0.4635 \times 10^{-13}$	$1.886 \times 10^{-13}$
0.82	26	0.03719	$0.2975 \times 10^{-13}$	$1.334 \times 10^{-13}$
2.50	12	0.04807	$0.3846 \times 10^{-13}$	$0.7638 \times 10^{-13}$