

# Atomic Ion Frequency Standards

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*Invited Paper*

*A new class of atomic frequency standard, based on ions trapped by electromagnetic fields, is under development. Such standards have the potential of achieving higher frequency accuracy than currently available standards. They are also capable of very good frequency stability. The history and status of trapped-ion frequency standards are reviewed. Prospects for future standards are discussed.*

## I. INTRODUCTION

Frequency standards based on trapped ions are still in a very early stage of development. Nevertheless, they appear to have some fundamental advantages over the more established types of frequency standards. Several reviews on ion traps and their application to frequency standards have already appeared [1]–[4].

In a trapped-ion frequency standard, the frequency of an oscillator is servoed to a resonance which corresponds to a transition between two energy levels of an atomic ion. The ions are suspended in space by a combination of electric and magnetic fields. In a conventional rubidium cell, the atoms are surrounded by a buffer gas having a pressure of about  $10^3$  Pa (approximately 10 torr). In an ion trap, the ions are held either in a vacuum or in a low-pressure buffer gas (less than  $10^{-3}$  Pa). In an atomic beam, the atoms also move through a vacuum, without collisions. However, the time available for interaction with the electromagnetic field is limited to their flight time through the apparatus, usually about 10 ms or less. Trapped ions can be observed for much longer periods.

Several types of trapped-ion frequency standards are currently under development. The  $^{199}\text{Hg}^+$  microwave frequency standard is the best developed [5]–[9]. Another frequency standard is based on a 303-MHz transition in  $^9\text{Be}^+$  [10]–[12]. Other microwave frequency standards are based on  $^{137}\text{Ba}^+$  [13] or  $^{171}\text{Yb}^+$  [14]. Optical frequency standards, based on narrow linewidth transitions in single trapped ions are being investigated [15]–[17]. They may

eventually have accuracies several orders of magnitude better than any present-day standards [18], [19].

## II. ION TRAPS

Two basic types of ion traps have been used in frequency standards. These are the Penning trap, also called the electromagnetic trap, and the Paul trap, also called the electrodynamic or radiofrequency (RF) trap [1], [3].

### A. The Penning Trap

The Penning trap uses static electric and magnetic fields. The electrostatic potential is

$$\phi(x, y, z) = A(x^2 + y^2 - 2z^2). \quad (1)$$

A typical electrode configuration used to create such a potential is shown in Fig. 1. The two endcap electrodes are held at the same potential relative to the ring electrode. The sign of  $A$  is such as to generate an electric field that forces the ion back toward the center if it is displaced in either direction along the  $z$  axis of the trap. However, if the ion is displaced radially (that is, in the  $xy$  plane) it is subjected to an electric force that forces it away from the center. Superimposing a sufficiently strong magnetic field confines the ions in all dimensions. A single ion undergoes simple harmonic motion along the  $z$  axis and a superposition of two circular motions in the  $xy$  plane. The higher-frequency motion is called the cyclotron motion; the lower-frequency motion is called the magnetron motion. The magnetron motion is a circular  $\vec{E} \times \vec{B}$  drift about the trap axis. Motion along the  $z$  axis is stable, because work has to be done to increase  $z^2$ . On the other hand, if the orbit of an ion is displaced radially outward, its potential energy *decreases*. Hence, energy conservation does not prevent the ions from being lost from the trap. However, conservation of  $L_z$ , the  $z$  component of the canonical angular momentum of the ions, leads to radial confinement [20]. In a real trap,  $L_z$  is only approximately conserved, because of collisions with neutral molecules and because of deviations of the trap electric and magnetic fields from cylindrical symmetry.

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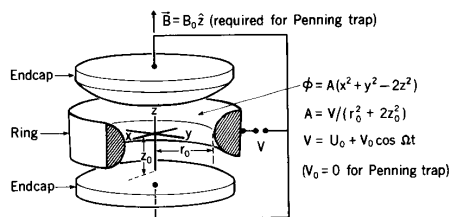


Fig. 1. Standard electrode configuration of a Penning trap or a Paul trap.

### B. The Paul Trap

A commonly used form of Paul trap, the RF quadrupole trap, uses an electrode configuration like the Penning trap (Fig. 1). Unlike a Penning trap, the electric potential applied between the electrodes oscillates at a high frequency. The parameter  $A$  in (1) has the form

$$A = \frac{U_0 + V_0 \cos \Omega t}{r_0^2 + 2z_0^2}. \quad (2)$$

Here,  $U_0$  and  $V_0$  are the static and RF potentials, and  $r_0$  and  $z_0$  are lengths that depend on the electrode geometry. Dynamic trapping is possible for some range of values of  $U_0$ ,  $V_0$ , and  $\Omega$ . With such values, the time-averaged force (the force averaged over a period of the oscillation) confines an ion in all dimensions. The static part of the electric potential can be adjusted to vary the ratio of the radial and axial restoring forces. The trajectory of an ion is a superposition of a driven motion at frequency  $\Omega$  and a low-frequency motion, due to the time-averaged force. The driven motion is called the micromotion and the low-frequency motion is called the secular motion.

Other types of RF trap may be useful in frequency standards. One is the linear RF trap. A schematic drawing is shown in Fig. 2. An RF potential is applied between the rods. The phase of the potential at each rod differs by  $180^\circ$  from that of the two that are nearest to it. This creates a time-averaged force which attracts an ion to the central axis. An electrostatic potential applied to the electrodes at the ends prevents the ions from escaping along the axis. In such a trap the RF fields approach 0 along a line rather than at only a point. In this trap the kinetic energy of the micromotion is less than in an RF quadrupole trap with the same number of ions and the same radial restoring force. Such a trap has recently been constructed for a frequency standard by Prestage *et al.* [21]. A “racetrack” trap can be made by connecting the ends of the rods into rings [22]. Recently, ions have been laser-cooled in a racetrack trap [23].

### III. ACCURACY AND STABILITY

Accuracy and stability are distinct properties of frequency standards. Accuracy refers to the absolute reproducibility of the frequency. In practice, it might be defined in terms of the frequency differences between independently constructed and operated standards of the same type. Stability refers to

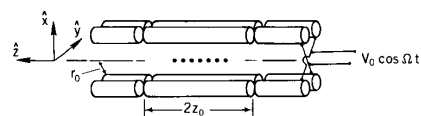


Fig. 2. Electrode configuration of a linear RF trap. Ions are trapped along the central ( $z$ ) axis.

the uniformity of the average frequency from one interval of time to the next.

#### A. Accuracy

The accuracy of a trapped-ion frequency standard depends on factors, such as collisions with background gas, perturbations due to external fields, and Doppler shifts, which can shift the resonance frequency of the ions.

In some cases, a buffer gas is deliberately introduced in order to cool the ions, and this leads to a frequency shift [24]. In the case of a frequency standard based on  $^9\text{Be}^+$  ions, variations in the background pressure of about  $10^{-8}$  Pa ( $10^{-10}$  torr) caused small but observable frequency shifts [12].

The shifts of hyperfine transition frequencies due to the electric fields present in a trap are small enough that they are not a serious problem [25]. This is because both levels are shifted by almost the same amount. Electric fields are more of a problem for frequency standards based on very narrow optical transitions. The rms electric field due to thermal (blackbody) radiation is about 8 V/cm at room temperature. This can cause a shift of an optical transition frequency of about one part in  $10^{16}$  from the frequency at 0 K [26]. Also, the energy of a state having an electric quadrupole moment could be shifted by the gradient of the electric field. Such a gradient could be caused by neighboring ions or by static charges on the trap electrodes [18].

The levels involved in the transition must be carefully chosen to avoid shifts due to fluctuating magnetic fields. These are transitions for which  $\partial\nu/\partial B$ , the first derivative of the frequency  $\nu$  with respect to the magnetic field  $B$ , approaches zero. For example, a transition between two  $m_F = 0$  sublevels ( $m_F$  is the quantum number of the  $z$  component of the total angular momentum  $F$ ) has this property at zero magnetic field. Penning traps are normally operated with magnetic fields of about 1 T. Fortunately, it is possible to find transitions in some ions for which  $\partial\nu/\partial B$  approaches zero at a value of  $B$  which is high enough to operate a Penning trap.

Cooling the ions is extremely important for reducing Doppler shifts of the resonances. Confinement of an atom to a region smaller than the resonance-radiation wavelength leads to a suppression of the first-order (linear in velocity) Doppler shift. This effect is called Dicke narrowing [27]. If an ion in a three-dimensional potential well is cold enough, its motion can be restricted to less than an optical wavelength, so Dicke narrowing occurs even for an

optical transition. Cooling directly reduces the second-order (quadratic in velocity) Doppler shift.

### B. Stability

The stability of a frequency standard is usually described by the sample variance of two successive measurements of the average frequency deviation [28]. This quantity is commonly called the Allan variance  $\sigma_y^2(\tau)$ , where  $\tau$  is the measurement time. The square root of the Allan variance typically has the form

$$\sigma_y(\tau) \approx \frac{K}{Q(S/N)} \propto \frac{1}{\sqrt{\tau}} \quad (3)$$

where  $K$  is a dimensionless constant of order 1,  $Q$  is the resonance frequency divided by the linewidth, and  $S/N$  is the signal-to-noise ratio for a measurement time  $\tau$ . In deriving the last part of (3), it was assumed that  $S/N$  is proportional to  $\tau^{1/2}$ . For all frequency standards,  $\sigma_y(\tau)$  eventually stops decreasing as  $\tau$  increases and may even start to rise.

The fundamental limitation on  $S/N$  is the statistical fluctuation in the number of ions that make a transition, when subjected to electromagnetic radiation near the resonance frequency. If the frequency is such that half the ions, on the average, make a transition, the fluctuation of the number is  $N_i^{1/2}/2$ , where  $N_i$  is the total number of ions [26].

The  $Q$  can be increased by increasing the time taken to drive the transition, since  $\Delta\nu$  is inversely proportional to this time. The time cannot be made much longer than the natural lifetime of the upper state, but for microwave transitions, this is not much of a limitation. The other way to increase  $Q$  is to increase  $\nu$ . Hence, there is interest in using narrow optical transitions in frequency standards.

### C. Accuracy-Stability Trade-Offs

For trapped-ion frequency standards, there is usually a trade-off between  $N_i$ , which limits the stability, and the second-order Doppler shift, which limits the accuracy. In a Penning trap, increasing  $N_i$  increases the average  $\vec{E} \times \vec{B}$  drift velocity of the ions, since the space charge increases the radial electric fields. In a Paul trap, increasing  $N_i$  increases the average velocity due to the micromotion, since the space charge forces the ions away from the center of the trap.

## IV. COOLING METHODS

Trapped ions can easily gain several electron volts of kinetic energy, or temperatures of thousands of kelvins, from electric fields in the trap. Since the ions are well isolated thermally from their environment, they do not quickly cool to room temperature. On the other hand, this thermal isolation makes it possible to cool the ions to less than 1 K in a room temperature apparatus, using a weak process like laser cooling.

### A. Collisional Cooling

Collisional cooling with neutral gas molecules is a simple way of cooling ions in a Paul trap [29]. Cutler *et al.* [24], [30] have collisionally cooled  $^{199}\text{Hg}^+$  ions in a Paul trap with helium gas. The secular motion was cooled to near room temperature, but the micromotion was hotter.

Collisional cooling with neutral atoms is not feasible for ions in a Penning trap. This is so because there is no restoring force in the radial direction. Collisions would quickly drive the ions out of the trap.

### B. Laser Cooling

Laser cooling is a very effective method for cooling certain kinds of ions to very low temperatures [31]–[33]. The basic idea is to irradiate the ions with light having a frequency slightly lower than that of a strong resonance line of the ion. Ions moving toward the source of the light absorb and reradiate photons at a high rate, because the Doppler shift brings the light closer to resonance. The ions lose energy, since they absorb the momentum of the photons. When the ions move away from the source of light, the Doppler shift is away from resonance, and photons are scattered at a low rate. The velocity is damped, on the average. The minimum temperature  $T$  that can be obtained in this manner is given by  $k_B T \approx \hbar\gamma/2$ , where  $k_B$  is Boltzmann's constant,  $\hbar$  is Planck's constant divided by  $2\pi$ , and  $\gamma$  is the radiative decay rate of the upper state. For typical cases,  $T$  is about 1 mK. This kind of laser cooling is called Doppler cooling, to distinguish it from other kinds of laser cooling [33].

Unfortunately, the nearly resonant light field perturbs the transition frequencies of the ion. One way of dealing with this problem is to turn off the light used for cooling for short periods. Another way is to simultaneously trap two kinds of ions. One kind of ion is continuously laser-cooled. It cools the other kind of ion by long range Coulomb collisions. The cooling radiation for one kind of ion does not perturb the resonance frequencies of the other kind very much. This cooling method, called sympathetic laser cooling, was studied by Larson *et al.* [34].

## V. RADIOFREQUENCY AND MICROWAVE FREQUENCY STANDARDS

In 1966, the  $\Delta F = \pm 1$  ground-state hyperfine transition of  $^3\text{He}^+$  was observed by Fortson *et al.* [35]. The method of detecting the resonance was based on collisions with Cs atoms whose electronic spins had been oriented by optical pumping with circularly polarized light. Resonances as narrow as 10 Hz were observed on a 8.666-GHz transition. This corresponded to a  $Q$  of almost  $10^9$ , about the same as that of a hydrogen maser. However, the second-order Doppler shift was relatively high and the  $S/N$  was relatively low, so this system was not developed further as a frequency standard.

### A. $^{199}\text{Hg}^+$ Paul Trap Frequency Standards

In 1973, Major and Werth observed the 40.5 GHz ground-

state hyperfine transition of  $^{199}\text{Hg}^+$  with a linewidth of a few Hz [36]. The  $Q$  of the resonance was approximately  $10^{10}$ .  $^{199}\text{Hg}^+$  has some basic advantages as a frequency standard. Its hyperfine transition has a very high frequency. Because of its large mass, it has a low second-order Doppler shift at a given temperature.

The detection of the resonance is based on optical pumping. The lowest electronic levels are shown in Fig. 3. The ground electronic state of  $\text{Hg}^+$  has the electronic configuration  $5d^{10}6s^2S_{1/2}$ . An RF-excited lamp containing the  $^{202}\text{Hg}$  isotope will emit 194 nm radiation that will drive  $^{199}\text{Hg}^+$  ions in the  $F = 1$  hyperfine level of the ground state to the  $5d^{10}6p^2P_{1/2}$  state. The ions can then decay to either the  $F = 0$  or  $F = 1$  hyperfine levels. The lamp eventually pumps most of the ions to the  $F = 0$  state. If microwave radiation near the 40.5-GHz resonance is applied, some ions are driven to the  $m_F = 0$  sublevel of the  $F = 1$  state. Then they can be excited to the  $5d^{10}6p^2P_{1/2}$  state by light from the lamp. When they decay, the 194-nm photons are detected with a photomultiplier tube.

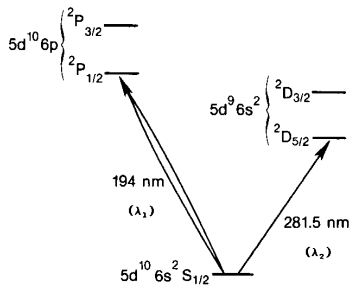


Fig. 3. Electronic energy levels of  $\text{Hg}^+$ . The ground electronic state of the  $^{199}\text{Hg}^+$  isotope is made up of two hyperfine levels, separated by 40.5 GHz. Some microwave frequency standards are based on this transition. An optical frequency standard might be based on the 281.5-nm transition.

Jardino *et al.* [5] made the first frequency standard based on this system. They measured  $\sigma_y(\tau) = 3.6 \times 10^{-11}\tau^{-1/2}$ , for  $10 < \tau < 3500$ , where  $\tau$  is the time interval in seconds. This stability was comparable to that of some commercial cesium atomic clocks.

This basic system was developed further by Cutler *et al.* [6], [7], [24], [30]. They introduced helium buffer gas to reduce the temperature of the ions. The lamp was turned off when the microwave radiation was applied, in order to avoid shifts of the microwave resonance frequency. The number of ions was about  $2 \times 10^6$ . The resonance linewidth was 0.85 Hz, so the  $Q$  was approximately  $5 \times 10^{10}$ . The results of a 115 day test showed fractional frequency fluctuations of  $7.6 \times 10^{-15}$  for integration times of 1 day [7]. A short term stability of  $\sigma_y(\tau) < 2 \times 10^{-12}\tau^{-1/2}$  can be inferred from the published data [7]. The frequency difference between two standards was between one and two parts in  $10^{-13}$ , which is an indication of their accuracy.

Prestage *et al.* [9] have demonstrated a  $^{199}\text{Hg}^+$  frequency standard based on a linear RF trap. Ramsey's separated oscillatory field method [37] was employed to drive the resonance. In this method, two short RF pulses are applied. This yields a linewidth in frequency (as opposed to angular frequency) units of about  $1/(2T)$ , where  $T$  is the time between the two pulses. This is about a factor of two narrower than is obtained by applying a single RF pulse of duration  $T$ . The frequency standard was operated with a linewidth of 0.16 Hz and a  $Q$  of  $2.5 \times 10^{11}$ . The short-term stability of the device was  $\sigma_y(\tau) = 1.6 \times 10^{-13}\tau^{-1/2}$  for  $50 < \tau < 800$ . Resonance linewidths as small as 0.03 Hz were observed when  $T$  was increased to 16 s. This corresponds to a  $Q$  of  $1.3 \times 10^{12}$ , the highest ever observed in a microwave atomic transition. A frequency standard based on a resonance line of this width could have a short term stability  $\sigma_y(\tau) = 5 \times 10^{-14}\tau^{-1/2}$ .

### B. $^9\text{Be}^+$ Penning Trap Frequency Standards

Bollinger *et al.* [10,11] demonstrated the first frequency standard based on laser-cooled ions. This standard was based on a 303-MHz hyperfine transition in the ground electronic state of  $^9\text{Be}^+$ . The hyperfine sublevels of the ground state are shown in Fig. 4. The first derivative of the frequency of the transition between the  $(m_I = -3/2, m_J = 1/2)$  sublevel and the  $(m_I = -1/2, m_J = 1/2)$  sublevel approaches zero at a value of the magnetic field near 0.8194 T. These levels are labeled "1" and "2" in Fig. 4. A frequency-doubled cw dye laser was used to generate 313-nm radiation to laser-cool and optically detect the ions.

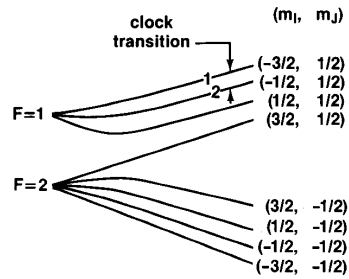


Fig. 4.  $^9\text{Be}^+$  energy levels in a magnetic field. The frequency standard is based on the 303 MHz "clock transition" between the levels labeled "1" and "2."

In the most recent version of the  $^9\text{Be}^+$  frequency standard, sympathetic laser cooling was used [12]. Magnesium ions were trapped at the same time and were continuously laser cooled. The number of  $^9\text{Be}^+$  ions was 5000 to 10 000. The 313-nm radiation source was tuned so that most of the ions would be pumped to the  $(m_I = 3/2, m_J = 1/2)$  ground-state sublevel in a few seconds. The 313-nm radiation was turned off, and ions in the  $(m_I = 3/2, m_J = 1/2)$  sublevel were transferred to the  $(m_I = 1/2, m_J = 1/2)$  sublevel

and then to the  $(m_I = -1/2, m_J = 1/2)$  sublevel by two successive RF pulses. The Ramsey method was then used to drive some of the ions to the  $(m_I = -3/2, m_J = 1/2)$  sublevel. Then RF pulses were applied in the reverse order, to bring ions which had remained in the  $(m_I = -1/2, m_J = 1/2)$  sublevel back to the  $(m_I = 3/2, m_J = 1/2)$  sublevel. The 313-nm source was then turned back on and the fluorescence intensity was measured. The intensity was proportional to the  $(m_I = 3/2, m_J = 1/2)$  population. If ions were left in the  $(m_I = -3/2, m_J = 1/2)$  sublevel, there was a decrease in the intensity. The time between the two RF pulses was as long as 550 s, although 100 s was more typical. With  $T = 550$  s, the width of the resonance was 900  $\mu$ Hz. The stability was better than  $3 \times 10^{-12} \tau^{-1/2}$  for  $10^3 < \tau < 10^4$ . However, there was a frequency shift with changes in pressure. This limited the long-term stability of the standard to about  $3 \times 10^{-14}$ . The uncertainty of the second-order Doppler shift, though, was only  $5 \times 10^{-15}$ . The longest time that the standard was operated continuously was about ten hours.

#### D. Other Work

Other ions have been investigated for use in microwave frequency standards. Lasers have been used for optical pumping and detection of hyperfine transitions in several other ions, including  $^{25}\text{Mg}^+$  [38],  $^{137}\text{Ba}^+$  [39],  $^{135}\text{Ba}^+$  [40],  $^{171}\text{Yb}^+$  [41], and  $^{173}\text{Yb}^+$  [42]. A frequency standard based on the 8-GHz hyperfine transition of  $^{137}\text{Ba}^+$  has shown a stability comparable to that of some commercial cesium standards [13]. A resonance with a  $Q$  of  $3.8 \times 10^{11}$  has been observed in  $^{171}\text{Yb}^+$ , which has a 12.6-GHz hyperfine transition. A  $^{171}\text{Yb}^+$  frequency standard has been tested, and a stability of  $\sigma_y(50\text{s}) = 2 \times 10^{-12}$  has been reported [14].

In general, frequency standards based on Penning traps suffer from the fact that the transitions which are insensitive to magnetic field fluctuations at high magnetic fields have low frequencies. Frequency standards based on Paul traps suffer from having high second-order Doppler shifts, due to the micromotion. Wineland *et al.* proposed to use a linear RF trap to confine a single string of ions, such as  $^{199}\text{Hg}^+$ , along the central axis [15]. The ions could be laser cooled and would have negligible micromotion. Such a standard might combine high accuracy and high stability.

## VI. OPTICAL FREQUENCY STANDARDS

An optical frequency standard might be based on a transition with a narrow natural linewidth. The  $Q$  could then be so high that the signal from even a single ion could yield good stability as well as good accuracy. The upper state of the transition must be metastable. Direct detection of the photons emitted by such a transition would be very difficult.

Sensitive detection of a single ion can be carried out by a double resonance method called electron shelving [18]. The  $\text{Hg}^+$  ion is an example of an atom that has a level structure that is suitable for this method (see Fig. 3). First, a pulse of resonant radiation is applied at wavelength  $\lambda_2$  to

try to drive the transition to the metastable state. Then, in a time less than the lifetime of the metastable state, another pulse of radiation is applied at wavelength  $\lambda_1$ . This radiation is resonant with a transition from the same lower state to a short-lived upper state. If the atom is shelved in the metastable state, no  $\lambda_1$  photons are emitted from the short-lived state. If the atom is in the lower state after the  $\lambda_2$  pulse, it can absorb and emit  $\lambda_1$  photons at a high rate. Thus the absorption of a single  $\lambda_2$  photon, which drives the atom to the metastable state, results in the absence of many  $\lambda_1$  photons. Thus individual  $\lambda_2$  transitions can be detected, even if not all of the  $\lambda_1$  photons are detected.

#### A. $\text{Ba}^+$ Single-Ion Optical Spectroscopy

The  $5d^2D_{3/2}$  and  $5d^2D_{5/2}$  states of  $\text{Ba}^+$  are metastable. Janik *et al.* observed a Doppler-free two-photon resonance between the ground  $6s^2S_{1/2}$  state and the  $5d^2D_{3/2}$  state in a single  $\text{Ba}^+$  ion in a Paul trap [43]. The two-photon resonance was 3-MHz wide because of the laser linewidths. The transition has the potential of being much narrower than 1 Hz, because of the long lifetime of the  $5d^2D_{3/2}$  state. Recently, the  $6s^2S_{1/2}$  to  $5d^2D_{5/2}$  one-photon transition has been observed in a single  $\text{Ba}^+$  ion, using electron shelving [17]. The width, which was limited by the laser, was about 50 kHz.

#### B. $\text{Hg}^+$ Single-Ion Optical Spectroscopy

$\text{Hg}^+$  has a level structure which is suitable for an optical frequency standard. The  $5d^96s^2\ ^2D_{5/2}$  state is metastable, with a lifetime of about 90 ms. The 194-nm transition from the ground  $5d^{10}6s^2S_{1/2}$  to the  $5d^{10}6p^2P_{1/2}$  state can be used for laser cooling and for detection by electron shelving. Some hyperfine components of the 281.5-nm transition in  $^{199}\text{Hg}^+$  are nearly independent of magnetic field, near zero field. One of these is the transition from  $F = 0$  in the ground state to  $(F = 2, m_F = 0)$  in the upper state. Recently, Bergquist *et al.* [16] observed this transition with a linewidth of under 80 Hz. The resonance line  $Q$  is over  $10^{13}$  and is the highest ever observed in an atomic transition. The laser frequency was servoed to the single-ion resonance for periods of several minutes [16]. Further work on this system might yield a frequency standard with  $\sigma_y(\tau) \approx 10^{-15} \tau^{-1/2}$  and accuracy of one part in  $10^{18}$  [15].

#### C. Other Work

Many other ions, including  $\text{Tl}^+$ ,  $\text{In}^+$ ,  $\text{Ga}^+$ ,  $\text{Al}^+$ ,  $\text{B}^+$ ,  $\text{Pb}^+$ ,  $\text{I}^+$ , and  $\text{Bi}^+$ , have narrow optical transitions, and have been proposed as frequency standards [18], [44]. Experimental work is being carried out on  $\text{Yb}^+$  [14], [45] and  $\text{Sr}^+$  [46]. Both  $\text{Yb}^+$  and  $\text{Sr}^+$  have been trapped and laser-cooled, but narrow optical lines have not been observed yet.

## VII. SUMMARY

Trapped-ion frequency standards are not yet in widespread operational use. The  $^{199}\text{Hg}^+$  microwave frequency standard has demonstrated good stability. Other frequency standards based on laser-cooled ions are being developed

and may be capable of better accuracy. Ultimately, the most accurate frequency standard may be based on an optical transition in a single, laser-cooled ion.

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