## CURRENT STATUS OF FREQUENCY CALIBRATION TABLES (0 TO 3000 CM-1)

#### FOR TUNABLE DIODE LASERS FROM HETERODYNE FREQUENCY MEASUREMENTS

J. S. Wells and M. D. Vanek
Time and Frequency Division
National Institute of Standards and Technology
(formerly National Bureau of Standards)
Boulder, Colorado 80303 USA

#### A. G. Maki

Molecular Spectroscopy Division National Institute of Standards and Technology Gaithersburg, MD 20899 USA

M. Schneider and A. Hinz<sup>+</sup>
Institut für Angewandte Physik
der Universität Bonn
D 5300 Bonn, West Germany

#### SUMMARY

The Time and Frequency Division of the National Institute of Standards and Technology (NIST), Boulder Laboratories, and the Molecular Spectroscopy Division of the NIST Gaithersburg Laboratories have collaborated over the past few years in an effort to provide accurate frequency calibration tables. This involves the use of heterodyne frequency measurements as well as the analysis and fitting of the infrared spectra of selected molecules. Of major interest are the linear triatomic molecules OCS and  $N_2O$ , which together cover a sizeable portion of the 0 to 3000 cm $^{-1}$  region. Some heterodyne frequency measurements can be made by locking a tunable diode laser (TDL) to an absorption feature of OCS, for example, and comparing the TDL frequency directly against a  $\rm CO_2$  laser frequency standard. However, most recent measurements have required a transfer oscillator to relate a frequency synthesized from  ${\rm CO_2}$  laser standards to the locked TDL frequency. The transfer oscillator for many of the measurements was a liquid-nitrogen-cooled CO laser. The transfer oscillator techniques and calibration tables resulting from the new frequency measurements on OCS and CS2 are presented. Current status of calibration tables is given for an interim OCS atlas, an  $N_2O$  atlas, and several other molecules of interest.

#### 1. INTRODUCTION

When the tunable diode laser (TDL) first became commercially available, the advertised resolution for these devices was orders of magnitude better than the accuracy of available frequency/wavenumber calibration standards. In response to the consequent need for improved

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calibration standards, the Molecular Spectroscopy Division in the NIST Gaithersburg Laboratories and the Time and Frequency Division in the NIST Boulder Laboratories initiated a joint program to provide calibration standards in the infrared region. The Molecular Spectroscopy Division had the requisite expertise for selection of appropriate molecules as well as for the analysis and fitting of the data. The Time and Frequency Division had a wealth of  ${\rm CO_2}$  laser standards, frequency measuring apparatus, and expertise remaining from frequency measurements involved in a determination of the speed of light.

Several criteria were established for these standards. First, in order to satisfy the largest number of potential users, it was decided that the most desirable types were absorption standards. A further restriction was made to those molecules that were easily handled. Since many TDLs exhibit a mode hop after tuning about 0.5 cm<sup>-1</sup>, a fiducial point every 0.5 cm<sup>-1</sup> was selected as a desirable feature. One of the more important aspects was for the molecule to have a simple spectrum (simple Hamiltonian); for example, it should display a relatively low line density and freedom from fine structure. The final criterion was a requisite number of transition frequencies good to 3 MHz. The last requirement was to be met by calculations based on constants determined in part from heterodyne frequency measurements traceable to CO<sub>2</sub> laser frequency standards.

Due to the limited number of heterodyne measurements possible, it was desirable to have information from supplementary sources such as microwave measurements. In some cases, TDL spectra which had been calibrated relative to bands determined from prior heterodyne measurements were useful. More recently, the TDL spectra have been supplanted by Fourier transform spectra (FTS) which were calibrated from the heterodyne measurements. The data from all of the various sources were weighted in proportion to the inverse square of the measurement uncertainty in the fitting processes.

Two molecules of major interest and utility have emerged over the last few years: carbonyl sulfide (OCS) and nitrous oxide (N $_2$ O). Both molecules have simple expressions for the energy values, typically (when the vibrational angular momentum is zero),

$$F(v,J) = E_v + B_v J(J+1) - D_v J^2 (J+1)^2 + H_v J^3 (J+1)^3 - L_v J^4 (J+1)^4, (1)$$

and the observed frequency for a particular transition is

$$v_{obs} = F(v', J') - F(v'', J'').$$
 (2)

When the vibrational angular momentum quantum number,  $\ell$  = 1, the energy values are given by

$$F(v,J) = E_{v} + B_{v}J(J+1) - D_{v}[J(J+1) -1]^{2} + H_{v}[J(J+1) -1]^{3}$$

$$+ 0.5[q_{v}J(J+1) - q_{v}J^{2}(J+1)^{2} + q_{v}J^{3}(J+1)^{3}].$$
(3)

We refer to papers cited in the references for more complicated cases. In most cases, the number of constants to be fitted for OCS and  $N_2O$  is comparatively small. We will describe OCS as a more detailed example and mainly list  $N_2O$  results in a companion fashion.

## 2. HETERODYNE MEASUREMENTS VS. A CO<sub>2</sub> LASER (860 TO 1110 CM<sup>-1</sup>)

In order to make heterodyne frequency measurements on a molecular band of interest, one must first determine which absorption features lie within a specified range (5 GHz, for example) of a CO<sub>2</sub> laser transition. Figure 1 indicates some relevant considerations.

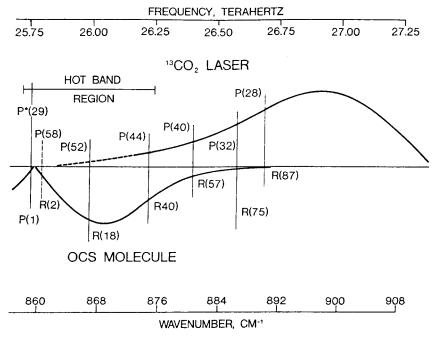


Fig. 1. Sketch of overlap between OCS R-branch and  ${\rm CO_2}$  laser P-branch.

Above the line is an envelope of the P branch of the  $^{13}\text{CO}_2$  laser; below is the R branch of the  $00^01$  -  $00^00$  band of OCS. At the very least, it is desirable to measure low-J P and R branch lines to determine the band center, mid-J lines for B-values, and a few high-J lines for centrifugal distortion constants. More generally, we aim for lines separated by about  $\Delta J = 10$ ; however some of these are not accessible due to holes in the TDL coverage. The vertical lines show overlaps for potential measurements, but the P(58) line would not lase. Fortunately, some hot-band transitions (indicated by the horizontal bar) lased, were subsequently measured, and then were used to measure the low-J OCS lines.

The heterodyne frequency measurements made against the  $\rm CO_2$  laser were straightforward. The TDL was locked to the OCS line of interest by a simple first derivative lock. In cases where the TDL mode did not have zero slope background, the lock was compensated to hold the midpoint of the derivative signal. The TDL and  $\rm CO_2$  laser outputs were heterodyned in a HgCdTe detector, and the resulting beatnote was measured by means of a spectrum analyzer and marker oscillator whose frequency was counted. The uncertainty in the measurement was taken as one-half the Doppler width divided by the signal-to-noise ratio of the lock signal plus one-tenth of the beat note linewidth on the spectrum

analyzer. Table I indicates partial results from some measurements on the  $00^{0}1$  -  $00^{0}0$ ,  $01^{1}e$ ,  $f_{1}$  -  $01^{1}e$ ,  $f_{0}$  and  $00^{0}2$  -  $00^{0}1$  bands of the most abundant isotope of OCS[1].

Table I. Heterodyne Frequency Measurements on OCS near 860 cm<sup>-1</sup>.

13 <sub>CO2</sub> Laser <sup>a</sup> Transition	OCS <sup>b</sup> Trans.	Diff. Freq.	OCS Frequency <sup>C</sup> MHz	0 C. MHz
P(28)	R(87)A	73.0	26674291.6(60)	0.4
P(32)	R(75)A	2773.8	26566226.9(30)	-0.1
P(38)	R(57)A	395.6	26393239.6(20)	-0.1
P(44)	R(40)A	1362.7	26218193.2(30)	0.0
P(52)	R(18)A	1733.6	25975344.4(20)	-1.8
P(25)*	R(7)A	-1668.0	25847177.1(20)	1.5
P(29)	P(1)A	-1277.5	25739018.1(20)	0.8
P(36)	R(84)B	174.0	26450485.5(30)	0.3
P(50)	R(42)B	-628.4	26034711.5(60)	0.2
P(25)*	R(25)B	-707.3	25848137.8(20)	-0.7
P(26)*	R(22)B	-1400.2	25814164.2(20)	1.1
P(50)	R(42)C	820.7	26036160.6(60)	-1.0
P(25)*	R(25)C	-34.5	25848810.6(40)	-0.2
P(26)*	R(22)C	-841.4	25814723.0(40)	-1.9
P(36)	R(86)D	600.4	26450911.4(30)	0.1
P(40)	R(73)D	-439.6	26334336.9(30)	-0.3
P(15)*	R(50)	810.7	26111131.5(40)	1.2
P(19)*	R(40)	85.0	26007511.5(40)	0.0
P(54)	R(31)	-329.0	25910930.4(60)	2.3
P(29)*	R(16)	2772.1	26743067.7(30)	-0.7

<sup>&</sup>lt;sup>a</sup>Transitions marked by an asterisk are from the  $01^11$  -  $[11^0$ ,  $03^10]_{\rm I}$  hot band. The others are the P<sub>I</sub> branch (lower frequency CO<sub>2</sub> band). <sup>b</sup>In the IAU-UPAP convention used here, A refers to the  $00^01$  -  $00^00$  band, B,C correspond to the  $01^{1e}$ ,  $f_1$  -  $01^{1e}$ ,  $f_0$  bands and D denotes the  $00^02$  -  $00^01$  band.

Measurements have also been made on other isotopic species of OCS. The natural abundance in un-enriched species is given in Table II. The observation of OCS lines in the TDL spectra (due to some of these isotopes) were not listed in our earliest calibration tables. We later obtained enriched samples for  $0\text{C}^{34}\text{S}$ ,  $0^{13}\text{CS}$ , and  $^{18}\text{OCS}$  and now have made measurements on the  $00^{01}$  -  $00^{00}$  bands of all six isotopic species listed in Table II as well as some hot bands[2,3]. The energy level diagram shown in Fig. 2 summarizes the measurements in the 860 cm<sup>-1</sup> region and gives the key to the band notation used in our pending OCS calibration atlas. Not all of the bands shown in the sample page of the atlas (Display I) are defined in Fig. 2. Additional band definitions will be supplied to any interested user requesting portions of the OCS atlas.

<sup>&</sup>lt;sup>c</sup>The estimated uncertainty in the last digits is given in parentheses.

Table II. Natural Abundances of Isotopic Carbonyl Sulfide.

Species	Abundance (%)
$0^{\text{CS}}_{0^{\text{C}}}^{34^{\text{S}}}_{0^{\text{C}}}^{34^{\text{S}}}_{0^{\text{S}}}^{0^{\text{S}}}_{0^{\text{CS}}}^{38^{\text{CS}}}_{0^{\text{C}}}^{13^{\text{C}}}_{0^{\text{C}}}^{34^{\text{S}}}$	93.7 4.2 1.1 0.75 0.2 0.05

(Note: We are now using the IAU-IUPAP notation in which the  $\nu_1$  and  $\nu_3$  bands are interchanged relative to the notation used by most workers. Even though we did not use this notation for some of our earlier papers, we adhere to the IAU-IUPAP notation in our current description of that earlier work.)

ENERGY LEVELS FOR CARBONYL SULFIDE (IAU-IUPAP Convention)

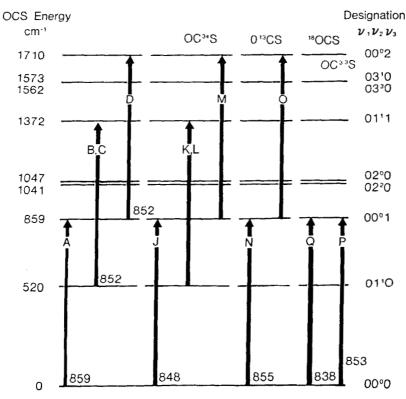


Fig. 2. Transitions in calibration tables in the  $797-893~{\rm cm}^{-1}$  region.

The accuracy and number of measurements for the A band were sufficient to generate a calibration table for the 815 to 892 cm<sup>-1</sup> region. This table was then used to calibrate about 85 supplementary TDL measurements for the B,C and D hot bands[2]. Display I shows a sample page from a multiband table covering the 797 to 893 cm<sup>-1</sup> region.

ATLAS OF INFRARED ASSORPTION LINES FOR OCS NEAR THE 860 CM(-1) BAND

```
1/CM (UNC) MHZ (UNC)
854.45408( 5)S 25615888.9( 14)
854.56673(18) 25619266.1( 54)
                                                                    ROT BAND ENERGY
                                                                    R(5)
                                                                                           526.51
                                                                                                           0.491-021
                                  25619266.1(54)
25619846.7(53)
25621178.3(19)
                                                                    R(22)
                                                                                         1474.92
                                                                                  н
                                                                                                          0.382-022
   854.58610(1h) 25621178.3(15, 854.63052(6) 25621394.6(46) 854.65317(6) 25621857.5(17) 854.66086(4) $25622088.1(11) 25622184.0(36) 25624253.2(52)
                                                                    R(22)
R(35)
                                                                                         1475.04
                                                                                                          0.382-022
                                                                                          769.05
                                                                                                          0.402-022
                                                                    R(23)
                                                                                         1159.35
                                                                                                          0.936-022
                                                                    R(46)
                                                                                          411.24
                                                                                                          0.132-022
                                                                    R(17)
R(35)
                                                                                            60.55
                                                                                                          0.630-021
  854.66406(12) 25622184.0(36)
854.73308(17) 25624253.2(52)
854.73405(17) 25624263.2(52)
854.75017(5)S 25624765.5(14)
854.76286(6)S 25625145.9(18)
854.79130(8) 25625998.6(24)
854.80633(5)S 25625449.0(16)
854.85306(5)S 25627733.5(14)
854.85306(5)S 256277923.3(6)
854.85511(2)S 25627923.3(6)
854.87161(3)S 25628466.2(10)
854.94391(18) 25630573.6(54)
854.98053(5) 25631191.0(53)
854.98053(5) 25631671.5(16)
854.98521(6) 25631811.9(19)
855.01810(15) 25632797.9(46)
                                                                                          769.31
                                                                                                          0.402-022
                                                                    R(22)
                                                                                        1144.08
                                                                                                          0.958-022
                                                                    R(22)
                                                                                        1144.09
                                                                                                          0.958-022
                                                                    R(18)
                                                                                 0
                                                                                          923.41
                                                                                                          0.510-023
                                                                   R(36)
                                                                                        1110.48
                                                                                                          0.157-022
                                                                   R( 3)
                                                                                             2.40
                                                                                                          0.335-022
                                                                   R( 6)
                                                                                 D
                                                                                          867.46
                                                                                                          0.224-021
                                                                   R( 6)
R( 6)
P(10)
                                                                                 В
                                                                                          528.94
                                                                                                         0.571-021
                                                                                                         0.571-021
                                                                                          528.95
                                                                                           22.31
                                                                                                         0.976-020
                                                                                              .00
                                                                   R( 0)
                                                                                                         0.120-022
                                                                                       1484.24
                                                                   R(23)
                                                                                 н
                                                                                                         0.381-022
                                                                   R(23)
                                                                                        1484.36
                                                                                 I
                                                                                                         0.381-022
                                                                  R(47)
R(36)
                                                                                         429.11
                                                                                                         0.124-022
                                                                                                         0.386-022
                                                                                         783.31
   855.01810(15)
                                 25632797.9(46)
                                                                   R(24)
                                                                                       1169.12
                                                                                                         0.930-022
  855.02019(11) 25632860.5(
855.03405(4)$ 25633276.0(
855.11089(6)$ 25635579.5(
855.11513(17) 25635706.7(
                                                                   R(36)
                                                         34)
                                                                                         783.58
                                                                                                        0.386-022
                                                                  R(18)
R(37)
R(23)
                                                                                                        0.643-021
                                                         11)
                                                                                           67.68
                                                         18)
                                                                                       1125.07
                                                                                                        0.150-022
                                                        52)
                                                                                Ε
                                                                                       1153.45
                                                                                                        0.956-022
  855.11626(17)
                                25635740.5( 52)
                                                                  R(23)
                                                                                       1153.45
                                                                                                        0.956-022
  855.12872(4)s 25638114.2(13)
855.18592(8) 25637829.0(24)
855.20093(5)s 25638279.0(15)
855.24637(5)s 25639641.2(14)
                                                                 R(19)
R(4)
R(7)
R(7)
                                                                                0
                                                                                        931.07
                                                                                                        0.518-023
                                                                                ρ
                                                                                            4.01
                                                                                                        0.415-022
                                                                                D
                                                                                        870.29
                                                                                                        0.253-021
                                                                                9
                                                                                        531.78
                                                                                                        0.647-021
 855.25095( 5)S 25639778.4( 14)
855.27206( 2)S 25640411.4( 6)
855.27362( 3)S 25640458.1( 10)
855.30674( 5) 25641451.1( 16)
855.31991(18) 25641845.7( 54)
                                                                  R( 7)
                                                                                        531.80
                                                                                                        0.647-021
                                                                 P( 9)
R( 1)
R(48)
                                                                                          18.26
                                                                                                        0.897-020
                                                                                N
                                                                                        .40
447.36
                                                                                                        0.239-022
0.116-022
                                                                                Q
                                                                 R(24)
                                                                                      1493.96
                                                                                                        0.379-022
 855.33876(6)
855.34175(17)
                                25642410.9(19)
                                                                  R(37)
                                                                               κ
                                                                                       797.96
                                                                                                      0.369-022
                               25642500.6( 52)
                                                                 R(24)
                                                                               I
                                                                                      1494.09
                                                                                                       0.379-022
 855.37519(11) 25643503.0(32)
855.39740(15) 25644169.0(45)
855.49603(3)$ 25644427.8(10)
855.45766(6)$ 25645975.6(18)
                                                                 R(37)
R(25)
R(19)
                                                                                        798.25
                                                                                                        0.369-022
                                                                                L
                                                                                                        0.921-022
                                                                               G
                                                                                      1179.29
                                                                                                       0.653-021
                                                                                         75.19
                                                                 R(38)
                                                                                      1140.06
                                                                                                       0.143-022
 855.49610(17)
                               25647128.0 52
                                                                               Ε
                                                                                                       0.951-022
                                                                 R(24)
                                                                                     1163.21
855.49610(17) 25647128.0(52)
855.49741(17) 25647167.1(52)
855.50602(4)$ 25647425.4(13)
855.57935(8) 25649623.5(24)
855.59430(5)$ 25650071.8(15)
855.63181(5) 25651196.4(16)
855.64244(5)$ 25651515.0(13)
855.64774(5)$ 25651673.8(14)
855.67442(3)$ 25652473.9(10)
855.68742(2)$ 25652863.4(6)
                                                                R(24)
R(24)
R(20)
R( 5)
R( 8)
R(49)
R( 8)
R( 8)
P( 8)
                                                                                      1163.22
                                                                                                       0.951-022
                                                                                                       0.523-023
                                                                              0
                                                                                       939.13
                                                                                           6.01
                                                                                                       0.494-022
                                                                                       873.53
                                                                                                      0.280-021
                                                                              D
                                                                                                       0.108-022
                                                                              Q
                                                                                       465.99
                                                                                                       0.719-021
                                                                                       535.03
                                                                              В
                                                                                                       0.719-021
                                                                              С
                                                                                       535.05
                                                                                                      0.358-022
                                                                                          1.21
                                                                                                      0.812-020
                                                                                         14.60
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Display I. Page from OCS multiband calibration atlas  $(855 \text{ cm}^{-1})$ .

The table lists the calculated values for the wavenumber and frequency (along with the calculated uncertainties) The transitions are designated by the rotational transition. transition and band designation (the more important bands are indicated in Fig. 2). Also given are the intensity and the lower state energy levels to permit the calculation of intensities at temperatures other than 296 K. The intensities have built into them the natural abundance of the isotopes occurring in a normal sample.

The intensity values are not presented as the final word, but are intended to provide relative intensities among the transitions listed. The value listed as A in the equation has units cm<sup>-1</sup>/molecules cm<sup>-2</sup> to conform to AFGL tapes. The transmission at the absorption peak is

given by

$$I = I_o \exp(-KLN_m),$$

where

$$K = [\Pi^{-1} \ln 2]^{1/2} A/b_D.$$

L is path length in cm,  $N_m$  is the concentration in molecules  $\mbox{ per cm}^3,$  and  $\mbox{b}_D$  is the Doppler width in  $\mbox{cm}^{-1}.$ 

The S listed after some of the wavenumber entries indicates transitions that are recommended for possible calibration standards. The spacing and relative intensities of lines in the immediate vicinity are used to identify unambiguously the standard frequencies. spectral regions, the OCS patterns are so similar in appearance that it is necessary to use an etalon to identify the line of interest. provides added motivation to make heterodyne measurements on the hot bands and the isotopic species.

Measurements have also been made on the  $2\nu_2$  (0200 - 0000) OCS band at 1040 cm<sup>-1</sup> and some hot bands in this same region[4,5]. multiband table (available on request) is recommended for the 1008 to 1092 cm<sup>-1</sup> region. Other direct measurements with a  $\rm CO_2$  laser include the  $10^{0}0$  -00<sup>0</sup>0 band of  $\rm N_20$  (978 to 1093 cm<sup>-1</sup>)[6] and some high J hot  $N_2O$  bands near 1107 cm<sup>-1</sup>[7].

## 3. HETERODYNE FREQ. MEASUREMENTS WITH A CO LASER (1220 to 1945 CM<sup>-1</sup>)

The next higher frequency region where we have made measurements was the 1257 to 1340 cm<sup>-1</sup> region. In this region, we rely on a transfer oscillator technique to relate the N2O frequencies of interest to the CO2 laser frequency standards. Each nitrous oxide measurement was a result of two nearly simultaneous measurements. The first measurement was a determination of the frequency of the CO laser relative to CO2 frequency standards; this could not have been possible without the use of the metal-insulator-metal (MIM) diode. The second was a measurement of the  $N_2{\rm O}$  transition of interest relative to the CO laser frequency. A detailed block diagram of the scheme is shown in Fig. 3.

The CO2 laser synthesizer consists of two stabilized CO2 lasers, a phase-locked microwave oscillator and frequency counter, a MIM diode, and rf components (amplifier, spectrum analyzer and synthesizer). First to be outlined is the measurement of the transfer oscillator frequency relative to the standard CO2 frequencies. radiation from the two stabilized CO2 lasers and a microwave oscillator onto the MIM diode, we generated currents in the diode at a synthesized frequency ve, given by

$$= \ell v_1 + m v_2 + n v_{Mw} \tag{4}$$

where  $v_1$  and  $v_2$  were the frequencies of the CO<sub>2</sub> laser standards and  $v_{Mw}$  was a microwave frequency. The quantities  $\ell$ , m, and n are integers which were allowed both positive and negative values. The synthesized  $v_s$  signals generally become weaker as the mixing order,  $[1+|\ell|+|m|+|n|]$ , increases. When the radiation from the CO laser,  $v_{CO}$ , was additionally coupled to the MIM diode, a beat note of frequency,  $v_{B1}$ , propagated from the diode, was amplified and then measured on the spectrum analyzer. The measured CO frequency was then

$$v_{CO} = v_s + v_{B1} = v_{xfer}. \tag{5}$$

The remainder of the measurement was a determination of the frequency difference,  $\nu_{B2}$ , between the CO laser frequency and the TDL frequency which was locked to the  $N_2O$  transition of interest. The molecular transition frequency,  $\nu_{mol}$ , was then

$$v_{mol} = v_{xfer} + v_{B2} = v_{NNO}. \tag{6}$$

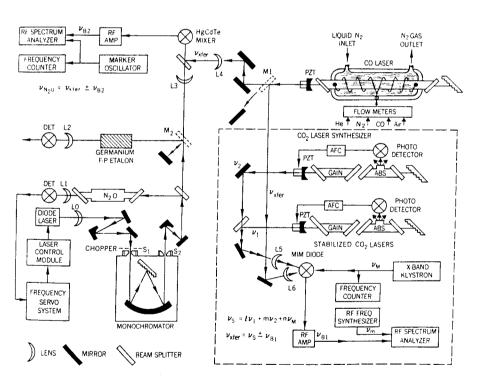


Fig. 3. Diagram of transfer oscillator scheme for CO laser region.

The work in the 1257 to 1340 cm<sup>-1</sup> region was particularly challenging because it involved operating on the high vibrational levels (v" ranged from 30 to 34) of a flowing-gas CO laser that was cooled by liquid-nitrogen. For the higher v" levels, the power levels were so low that it was sometimes difficult to couple usable power to the MIM diode. In spite of this difficulty, 47 N<sub>2</sub>O frequency measurements were made in this region[8,9], and a 1600 entry calibration table is available.

In order to indicate the synthesis in some detail, we discuss some measurements of carbon disulfide (CS2) transitions as an example of the work with the transfer oscillator scheme. Since the region of interest for the CS<sub>2</sub> work was between 1460 and 1550 cm<sup>-1</sup> the objective of this experiment was to synthesize frequencies in the 43.8 to 46.5 THz region. In an effort to keep the mixing order (more particularly, [|l|+|m|] low, we have been constrained to use the highest band of frequencies for the  $\nu_1$  laser transition (the  $R_{TI}$  band of the  $^{18}0^{12}\text{C}^{18}\text{O}),$  and the lowest band of frequencies for the  $\nu_2$  transitions (the  $P_T$  band of  $^{16}O^{13}C^{16}O$ ). While other combinations ( $\ell = 4$  and m = 1-2, for example) will work to synthesize some of the frequencies, a choice of  $\ell = 3$  and m = -2 will permit synthesis of most of the frequencies needed without the inconvenience of changing to different  ${\rm CO}_2$  lasers. The various n values selected were restricted to 0, +1 , and  $\pm$  2, and a single X-band klystron sufficed for the microwave requirements. The difference (between the synthesized frequency and the transfer oscillator frequency) frequency,  $v_{B1}$ , was amplified and then measured with respect to an rf synthesizer. The frequency of the transfer oscillator was then as given by eq. (5) above.

The second part of the procedure was a difference frequency measurement between the CO laser transfer oscillator and a TDL whose frequency was locked to the CS $_2$  transition of interest. The frequency of the CS $_2$  transition was then given by eq. (6) where the beat frequency,  $\nu_{\rm B2}$ , was observed on a microwave spectrum analyzer and measured with a marker oscillator whose frequency was counted. The measurements are given in Table III, which for each carbon disulfide frequency measurement lists the CO $_2$  laser transitions which oscillate at the frequencies  $\nu_1$  and  $\nu_2$ , the microwave frequency, the two beatnote frequencies,  $\nu_{\rm B1}$  and  $\nu_{\rm B2}$ , and the values for the CO and CS $_2$  frequencies.

A 1.7 m cell was used for the measurements and the pressures were all the order of 10 Pa  $(0.08\ \text{Torr})$  or less. The carbon disulfide sample was enriched in carbon-13 to provide an equal mixture of both carbon isotopes.

As indicated by the O.- C. (Observed - Calculated) column in Table III, the fit is equal to our best previous work. Two factors permit this result, which is better than some of our other recent work. First, the absorption lines were quite strong and permitted good signal-to-noise ratios for the lock signal. Perhaps even more important was the relatively narrow jitter linewidth of the TDL used for these measurements (compared to TDLs available for much of our work).

The constants derived from this work were used to calculate calibration tables covering the 1460 to 1550 cm<sup>-1</sup> region[10].

Table III. Heterodyne Frequency Measurements on Carbon Disulfide.

Synthesis Scheme			Transfer Oscillator Carbon Disulfi		arbon Disulfide	de	
lxT(v <sub>1</sub> ) <sup>a</sup>	+ mxT(v <sub>2</sub> ) <sup>a</sup>	+ nxv <sub>H=</sub> +v <sub>B1</sub>	CO Trans Pv"(J")		Trans.	Frequency, MHz	0 C., MHz
3x8R <sub>II</sub> (10)	- 2x <sup>3</sup> P <sub>I</sub> (10)	+ 2x9000 +725.8	P25(13)	43855934.8 <sup>b</sup>	13CS <sub>2</sub> P(82) +827.9	43856762.7(30)°	0.5
3x <sup>8</sup> R <sub>II</sub> (16)	$-2x^{3}P_{1}(6)$	- 2x10500 +904.4	P25(12)	43957232.4	P(72) -3827.7	43953404.7(30)	-0.1
3x8R <sub>II</sub> (18)	- 2x <sup>3</sup> P <sub>I</sub> (12)	- 1x10000 +966.8	P24(15)	44372051.8	P(22) -3619.8	44375671.6(30)	-2.0
3x8R <sub>11</sub> (16)	- 2x <sup>3</sup> P <sub>I</sub> (16)		P24(14)	44476365.2	P(8) -751.6	44475613.6(20)	0.3
3x <sup>8</sup> R <sub>II</sub> (16)	- 2x <sup>3</sup> P <sub>I</sub> (20)		P24(12)	44682033.9	R(24) -2729.7	44679304.2(30)	1.1
3x <sup>8</sup> R <sub>11</sub> (20)	- 2x <sup>3</sup> P <sub>I</sub> (18)		P24(11)	44783379.9	R(44) -2516.8	44780863.1(30)	1.1
3x <sup>8</sup> R <sub>II</sub> (18)	$-2x^3P_1(22)$		P24(10)	44883726.3	R(68) -2917.5	44880808.8(50)	-2.6
3x <sup>8</sup> R <sub>II</sub> (20)	- 2x <sup>3</sup> P <sub>I</sub> (22) -		P24(9)	44983071.0	R(102) -1817.5	44981253.5(30)	0.0
					12 CS <sub>2</sub>		<del></del>
3x <sup>8</sup> R <sub>II</sub> (20)	$-2x^3P_1(22)$	2x10000 -294.1	P24(9)	44983071.0	P(116) +3894.3	44986965.3(20)	0.9
3x8R <sub>II</sub> (22)	$-2x^3P_1(22)$	1x11500 -832.7	P23(15)	45095970.6	P(106) +3132.6	45099103.2(50)	2.3
3x <sup>8</sup> R <sub>II</sub> (26)	$-2x^3P_{I}(24)$		P23(12)	45409085.8		45410368.2(30)	0.1
3x <sup>8</sup> R <sub>II</sub> (30)	$-2x^3P_1(28)$ -		P23(8)	45812635.1		45813975.8(40)	-2.5
3x <sup>8</sup> R <sub>II</sub> (34)	$-2x^3P_1(26) +$		P22(14)	45928609.7		45933333.0(20)	-1.1
0x8R <sub>II</sub> (30)	- 2x <sup>3</sup> P <sub>I</sub> (32) -	2x10500	P22(13)	46034027.1		46035322.3(30)	0.2
$1x^3 P_1 (34) -$	1x8R <sub>II</sub> (30) -	-575.5 2x9000 -299.0	P21(16)	46442404.9		46438997.8(70)	5.2

<sup>&</sup>lt;sup>a</sup>The left superscript indicates the  $CO_2$  isotope; 8 indicates  $^{12}C^{18}O_2$  and 3 is for  $^{13}C^{16}O_2$ . bWe estimate that the CO freq. represents the center of the transition to within 3 MHz. The uncertainty as a transfer oscillator is 0.2 MHz and is included in the  $CS_2$  uncertainty. The uncertainty in the last digits is given in parentheses.

The liquid-nitrogen-cooled CO laser was also recently used to measure the  $01^11$  -  $00^00$  and  $02^01$  -  $01^10$  bands of OCS at 1370 cm<sup>-1</sup>[11], and the  $10^00$  -  $01^10$  band of  $N_2O$  at 1635 cm<sup>-1</sup>[12]. In both instances the bands designated were too weak to be useful for calibration, but were useful for determining bands which were not within our direct measurement capabilities. We will defer discussion of these bands until later.

The  $00^{\circ}2$  -  $00^{\circ}0$  band of OCS has been determined by indirect measurements [1], and also by measurements with a sealed-off CO laser which was cooled by a mixture of dry-ice and alcohol [3]. A single band (A band) calibration table covering the 1662 to 1725 cm<sup>-1</sup> has been published [1], and 45 new measurements in this region have just been completed[13]. One motivation for the new measurements was to improve

the existing calibration table, although the adjustment on the A band is in the 1 MHz range. Most of the measurements are on hot bands and isotopic species and one use will be to upgrade a multiband table in the calibration atlas. The bands involved in the new measurements are shown in Fig. 4, an energy level diagram which indicates the transitions primarily in the  $1700~\rm cm^{-1}$  region.

Earlier measurements that used the sealed-off CO laser included the  $01^11$  -  $00^00$  band of  $N_20$ ; they provided for a calibration table covering the 1834 to 1918 cm<sup>-1</sup> region[7]. More recently this system was used to measure the  $02^01$  -  $00^00$  band of OCS and a single band calibration table covering 1866 to 1919 was published[14]. Subsequently, about 50 isotopic and hot band measurements were made in the same region[15]. These will be used to upgrade a multiband table in the calibration atlas and to provide for tables outside the region described so far.

# ENERGY LEVELS FOR CARBONYL SULFIDE (IAU-IUPAP Convention)

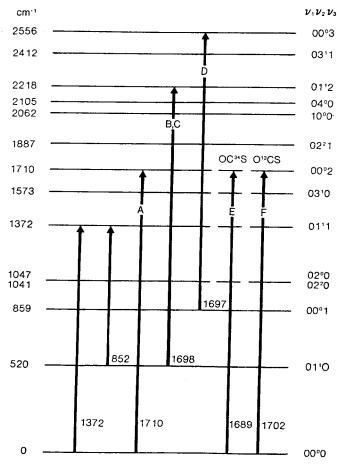


Fig. 4. Energy levels for OCS transitions in the  $1700~{\rm cm}^{-1}$  region.

We conclude the directly measured results with a reference to some measurements made with a color center laser whose frequency was synthesized in the same fashion by combining  ${\rm CO}_2$  harmonics in a MIM diode. Measured were the  $00^02$  -  $00^00$ ,  $20^01$  -  $00^00$ , and  $12^00$  -  $00^00$  bands of N<sub>2</sub>O. These results permitted calibration tables covering the regions; 4341 to 4442, 4573 to 4661, and 4670 to 4755 cm<sup>-1</sup>[16].

#### 4. CALIBRATION TABLES OUTSIDE THE REGION OF HETERODYNE MEASUREMENTS

All of the TDL measurements described here were made in regions where the CO or  ${\rm CO_2}$  lasers (with the useful isotopic variations) operate. Some measurements were made to provide information which indirectly determined energy levels required for calibration tables. We refer again to the OCS energy level diagram in Fig 4. The measurements of the OCS  $01^{1}1 - 00^{0}0$  band at 1373 were combined with

### ENERGY LEVELS FOR CARBONYL SULFIDE

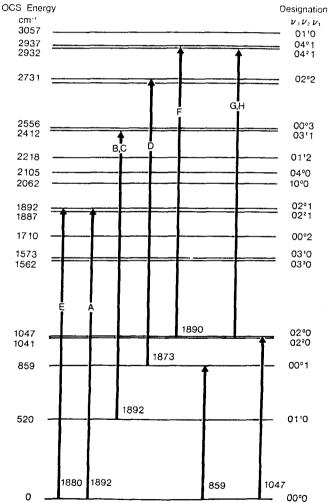


Fig. 5. Energy levels for OCS transitions in the 1900 cm<sup>-1</sup> region.

some hot band measurements of the  $01^11$  -  $01^10$  band at  $860~\rm cm^{-1}$  to provide constants for the  $01^10$  level at  $520~\rm cm^{-1}$  and a subsequent calibration table covering the  $480~\rm to$   $550~\rm cm^{-1}$  region. With the constants for the  $01^10$  level established, B and C hot band measurements at  $1700~\rm cm^{-1}$  permit constants to be determined for the  $01^12$  level and a calibration band to be calculated for the  $2218~\rm cm^{-1}$  region. The D hot band at  $1700~\rm cm^{-1}$  can be combined with the measured value of the  $00^01$  level at  $859~\rm cm^{-1}$  to yield constants for the  $00^03$  level and a subsequent table for the  $2556~\rm region$ .

Similar results are obtained from the 1890 cm $^{-1}$  hot bands shown in OCS energy level diagram in Fig. 5. (The E band refers to the  $\rm OC^{34}S$  isotope.) The energy levels at 859 and 1047 cm $^{-1}$  were determined from direct  $\rm CO_2$  laser measurements. With these starting energies determined, the 1873 cm $^{-1}$  D hot band measurements determine the  $\rm O2^{02}$  level at 2731 cm $^{-1}$ , and the 1890 cm $^{-1}$  F band measurements determine the 04 $^{01}$  level at 2937 cm $^{-1}$ . Single band tables covering the 2695 to 2762 and 2915 to 2963 cm $^{-1}$  are now available[15].

The same general approach was applied to  $N_2O$ . We do not cover the results in detail, but we indicate the measured bands all together in the  $N_2O$  energy level diagram (Fig. 6) shown below.

## Energy Levels for N2O

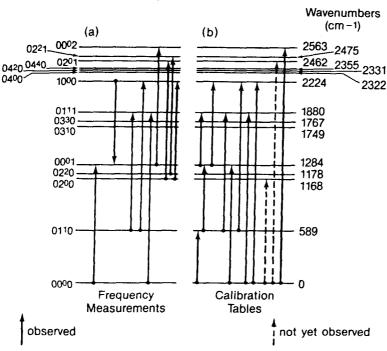


Fig. 6. Energy levels and measured transitions for nitrous oxide.

Figure 7 gives a quick indication of the wavenumber regions covered. A summary of availability (Table IV) indicates the extent of calibration standards and points out where coverage for a specific

region may be found. The OCS atlas is not completed at this time, but portions are available from either Maki or Wells on request for specific regions.

Additional work has been done on a few other molecules to fill in some gaps and provide alternate molecules in a few instances. Included in this category are deuterium bromide[17] and nitric oxide[18].

# Calibration Standards Available from Frequency Measurements

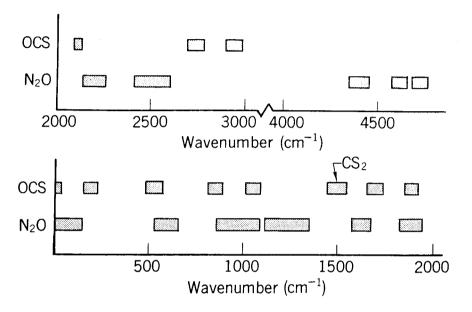


Fig. 7. Coverage afforded by carbonyl sulfide and nitrous oxide.

#### ACKNOWLEDGEMENTS

The results which we have presented also rely in part on the published work of many researchers. Their contributions are cited in the papers in the references section. Our work would not have been possible without the early contributions of the late F. R. Petersen. The parallel work on OCS by A. Fayt on OCS was especially useful. We are also indebted to D. A. Jennings for his valuable contributions with computer programs and other helpful input. This program has had the continuing support of the NASA Upper Atmospheric Research Office.

#### AVAILABILITY SUMMARY

	-	h 1	A 1 T - L T	E	Calibration.

Waver		er Region	Molecule	Band	Availability
1	to	207 cm <sup>-1</sup>	DBr	(rotational)	Ref. [17]
488	to	557	OCS	$01^{1}0-00^{0}0$	Ref. [11]
520	to	660	$N_2O$	$01^{1}0-00^{0}0$	Ref. [12]
797	to	893	oĉs	multiband	on request <sup>a</sup>
815	to	892	ocs	00 <sup>0</sup> 1-00 <sup>0</sup> 0	Ref. [1]
978	to	1093	$N_2O$	$10^{0}0-02^{0}0$	Ref. [6]
1008	to	1092	očs	multiband	on request
1105	to	1238	N <sub>2</sub> O	02 <sup>0</sup> 0-00 <sup>0</sup> 0	Ref. [6]
1207	to	1340	NaO	$00^{0}1-00^{0}0$	Ref. [8]
1460	to	1550	13 <sub>CS2</sub> , CS2	$00^{0}1-00^{0}0$	Ref. [10]
1594	to	1992 <sup>b</sup>	DBr	1-0	Ref. [17]
1649	to	1738	OCS	multiband	on request
1661	to	1738	OCS	00 <sup>0</sup> 2-00 <sup>0</sup> 0	Ref. [1]
1816	to	1930	N <sub>2</sub> 0	$01^{1}1-00^{0}0$	Ref. [8]
1834	to	1918	$N_2^-$ O	$01^{1}1-00^{0}0$	Ref. [7]
1845	to	1921	ocs	multiband	on request
1864	to	1920	OCS	$03\frac{1}{9}1-01\frac{1}{9}0$	Ref. [15]
1866	to	1919	OCS	$02^{0}1-00^{0}0$	Ref. [14]
2013	to	2139 <sup>c</sup>	OCS	multiband	on request
2135	to	2268 <sup>C</sup>	N <sub>2</sub> O	10 <sup>0</sup> 0-00 <sup>0</sup> 0	Ref. [8]
2409	to	2508	$N_2^{-}$ 0	$02^{0}1-00^{0}0$	Ref. [6]
2490	to	2605	$N_{2}^{-}O$	$00^{0}_{2}$ $-00^{0}_{0}$	Ref. [9]
2695	to	2762	oĉs	$02^{0}2-00^{0}0$	Ref. [15]
2915	to	2963	ocs	$04^{0}_{1}-00^{0}_{0}$	Ref. [15]
4341	to	4442	N <sub>2</sub> O	20 <sup>0</sup> 0-00 <sup>0</sup> 0	Ref. [16]
4573	to	4661	$N_2^{2}$ 0	12 <sup>0</sup> 1-00 <sup>0</sup> 0	Ref. [16]
4670	to	4755	N <sub>2</sub> O	$10^{0}2-00^{0}0$	Ref. [16]

<sup>a</sup>Available from either A. G. Maki of the Molecular Spectroscopy Division, National Institute of Standards and Technology, Gaithersburg, Maryland 80899 or J. S. Wells, Time and Frequency Division, National Institute of Standards and Technology, Boulder, Colorado 80303.

 $^{\mathrm{b}}\mathrm{The}$  spectrum consists of closely spaced pairs (0.5 cm $^{-1}$ ) of lines repeated every 11 acm $^{-1}$ .

<sup>c</sup>These bands are not based on heterodyne frequency measurements at this time. We hope to make measurements in the 2000 to 2300  $\rm cm^{-1}$  region during the coming year.

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