# Tunable Laser Diode Study of the $\nu_{3}$ Band of $\mathrm{SiF}_{4}$ near $9.7 \mu \mathrm{~m}^{1}$ 

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Doppler-limited tunable-diode laser spectra of the stretching fundamental $\nu_{3}$ of ${ }^{28} \mathrm{SiF}_{4}$ near $1031 \mathrm{~cm}^{-1}$ were analyzed and the spectroscopic constants determined. The $\nu_{3}$ vibrational dipole moment derivative was determined for several rovibrational lines.

## INTRODUCTION

The $\nu_{3}$ mode of $\mathrm{SiF}_{4}$ has stimulated recent interest since multiple-photon dissociation occurs when this mode is pumped by a high-power $9.4-\mu \mathrm{m} \mathrm{CO}_{2}$ laser ( 1 ). The various experiments involving pumping the $\nu_{3}$ band of $\mathrm{SiF}_{4}$ with a $\mathrm{CO}_{2}$ laser include saturation spectroscopy (2-4), photon echoes (5,6), laser-induced fluorescence and dissociation ( $7-10$ ), and silicon isotope separation (11). A full understanding of these effects depends on the identification of the detailed rovibrational structure of $\mathrm{SiF}_{4}$ that is nearly resonant with $\mathrm{CO}_{2}$ laser frequencies (12). Such information is not extractable from the previous low-resolution band-contour studies of the $\nu_{3}$ band (13-16).

We report here a high-resolution Doppler-limited analysis of the $\nu_{3}$ band of ${ }^{28} \mathrm{SiF}_{4}$ between 1023 and $1038 \mathrm{~cm}^{-1}$. This is the first step necessary for an understanding of the $\nu_{3}$ vibrational ladder and the multiple-photon absorption process. We have assigned most ground-state transitions in the above range corresponding to $R(60)$ $P(60)$. A total of 215 of the assigned transitions were used in a least-squares fit to a 10 -parameter model Hamiltonian, giving an overall standard deviation of 6 $\times 10^{-4} \mathrm{~cm}^{-1}$. For several lines in the $R$ branch, where our instrumental resolution was sub-Doppler, we have determined the vibrational transition dipole from intensity measurements.

## EXPERIMENTAL DETAILS

The $\nu_{3}$ band of $\mathrm{SiF}_{4}$ was recorded using $\mathrm{Pb}_{1-x} \mathrm{Sn}_{x} \mathrm{Te}$ semiconductor diode lasers in spectrometers whose characteristics have been described previously (17-20). The

[^0]sample was cooled to $170-200 \mathrm{~K}$ to suppress hot-band structure. The frequencies of lines used in the fit of the spectroscopic constants were measured using a doublebeam system (19) in which the $\mathrm{SiF}_{4}$ spectrum and that of a calibrating gas were recorded simultaneously. Immediately before or after each such run, interference fringes from a germanium etalon (free spectral range $0.0165 \mathrm{~cm}^{-1}$ ) were recorded to establish the diode tuning rate. All lines selected for measurement were within $\pm 0.1 \mathrm{~cm}^{-1}$ of a calibration feature of $\mathrm{CO}_{2}$ (21) or OCS (17). Repeated determinations of the frequencies of several lines indicated that the measurements are accurate to within $\pm 0.001 \mathrm{~cm}^{-1}$. For the determination of the transition dipole moment, $\mathrm{SiF}_{4}$ pressures were measured using a capacitance manometer to better than $5 \%$.

## ASSIGNMENTS AND ANALYSIS

The transition frequencies in a dipole-active fundamental of a spherical-top molecule can be expressed in the diagonal approximation as (22-24)
$P$ branch:
$\nu_{P}\left(J, C^{n}\right)=m-n J+p J^{2}-q J^{3}+s J^{4}+\left[g+h J+k J^{2}\right] \bar{F}(4)+z^{\prime} \bar{F}(6)$,
$Q$ branch:

$$
\begin{align*}
\nu_{Q}\left(J, C^{n}\right)=m+v J(J+1)+w J^{2}(J & +1)^{2} \\
& +[-2 g+u J(J+1)] \bar{F}(4)-2 z^{\prime} \bar{F}(6) \tag{1b}
\end{align*}
$$

$R$ branch:

$$
\begin{align*}
\nu_{R}\left(J, C^{n}\right)=m+n(J+1)+p(J & +1)^{2}+q(J+1)^{3}+s(J+1)^{4} \\
& +\left[g-h(J+1)+k(J+1)^{2}\right] \bar{F}(4)+z^{\prime} \bar{F}(6) \tag{1c}
\end{align*}
$$

with the off-diagonal terms in the Coriolis submatrices neglected. The index $C$ designates the tetrahedral species with counting index $n$ for repeated species within each ground state angular momentum $J$. The $\bar{F}(4)$ and $\bar{F}(6)$ are products of sym-metry-adapted fourth- and sixth-rank tensor coefficients. These have been calculated by Krohn (25) for all $C^{n}$ up to $J=150$.

These formulas were sufficient for making line assignments in the $P, Q$, and $R$ branches for $J \leq 40$. However, for assigning lines corresponding to higher- $J$ transitions it was necessary to include the off-diagonal Coriolis submatrices and calculate the "off-diagonal corrections" (26). To calculate these corrections, we diagonalized the full Coriolis energy matrix for each $J^{\prime}$ of $\nu_{3}$. For this purpose it was necessary to add the appropriate ground-state energies

$$
\begin{equation*}
E_{0}=B_{0} J(J+1) \tag{2}
\end{equation*}
$$

to the transition frequencies in Eq. (1) before diagonalizing, where

$$
J^{\prime}= \begin{cases}J-1 & P \text { branch }  \tag{3}\\ J & Q \text { branch } \\ J+1 & R \text { branch. }\end{cases}
$$

One may then define the $\nu_{3}$ scalar parameters from the spectroscopic parameters of Eqs. (1) to be

$$
\begin{align*}
m & \sim \nu_{3}-2\left(B \zeta_{3}\right),  \tag{4a}\\
n & \sim B_{3}+B_{0}-2\left(B \zeta_{3}\right),  \tag{4b}\\
Z_{3 s} & \sim p-v,  \tag{4c}\\
Y_{3}=B_{3}-B_{0} & \sim(v+2 p) / 3 . \tag{4d}
\end{align*}
$$

The $\nu_{3}$ scalar energies for each $J^{\prime}$ then become
$E_{P}=\nu_{3}+2\left(B \zeta_{3}\right) J^{\prime}+B_{3} J^{\prime}\left(J^{\prime}+1\right)-Z_{3 s}\left(J^{\prime}+1\right)^{2} / 3$

$$
\begin{equation*}
-q\left(J^{\prime}+1\right)^{3}+s\left(J^{\prime}+1\right)^{4} \tag{5a}
\end{equation*}
$$

$E_{Q}=\nu_{3}-2\left(B \zeta_{3}\right)+B_{3} J^{\prime}\left(J^{\prime}+1\right)+2 Z_{35} J^{\prime}\left(J^{\prime}+1\right) / 3+w\left(J^{\prime}\right)^{2}\left(J^{\prime}+1\right)^{2}$,
$E_{R}=\nu_{3}-2\left(E \zeta_{3}\right)\left(J^{\prime}+1\right)+B_{3} J^{\prime}\left(J^{\prime}+1\right)-Z_{3 s}\left(J^{\prime}\right)^{2} / 3+q\left(J^{\prime}\right)^{3}+s\left(J^{\prime}\right)^{4}$.
Including the tensor terms in the $\nu_{3}$ matrix for a given $J^{\prime}$ along with the above scalar terms and diagonalizing results in the $\nu_{3}$ rovibrational energies. Subtracting the ground-state energies gives us accurate transition frequencies. For the accuracy needed, it was not necessary to include the quartic scalar term $D_{0} J^{2}(J+1)^{2}$ explicitly in the ground-state energy although it is implicit in the spectroscopic parameters $q, s$, and $w$.
In order to least-squares fit the calculated transition frequencies to the data, it is necessary to determine the derivative of the $\nu_{3}$ matrix eigenvalues (energies) with respect to each parameter. Although in most cases the diagonal terms in the matrix can be taken, it is sometimes necessary to use the expectation value in the energy eigenbasis according to the Feynman-Hellman theorem. From this latter procedure we were able to fit $B \zeta_{3}$ due to the dependence of the off-diagonal corrections on this parameter.

Complete assignments were made from $R(60)$ to $P(60)$ in the range 1023-1038 $\mathrm{cm}^{-1}$ for which we had continuous diode coverage. We used 215 lines in the fit which were usually unblended and were always within $\pm 0.1 \mathrm{~cm}^{-1}$ of a $\mathrm{CO}_{2}$ or OCS calibration feature. In cases where a line consisted of an unresolved cluster of several transitions, only one member was used in the fit. This member corresponded to that closest to the spin statistically weighted center of gravity when blending was significant. Included among the 215 lines are lines identified in the ${ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ saturation spectra (12) taken with a waveguide laser (27).

In Table I are listed the rovibrational transitions used in the fit along with their measured frequencies. A fit to the data in Table I using Eqs. (1), (2), and (5) resulted in the determination of the 10 spectroscopic constants listed in Table II. The constants $u$ and $z^{\prime}$ were too small to be determined. Also listed in Table II are constants derived according to Eqs. (4).

The Coriolis constant $B \zeta_{3}$ was fixed at a value consistent with Eq. (4b) when the value for $B \sim B_{3} \sim B_{0}=0.13814(36) \mathrm{cm}^{-1}$ was derived from electron diffraction data (28). Since the constant $n$ is very well determined, the error for $B \zeta_{3}$ is basically

TABLE I
Observed and Calculated Transition Wavenumbers in $\nu_{3}$ of ${ }^{28} \mathrm{SiF}_{4}$

| Line | C | $\mathrm{n}^{\text {a }}$ | $\nu_{\text {obs }}, \mathrm{cm}^{-1}$ | $\Delta^{b}$ | Line | C | $\mathrm{n}^{\text {a }}$ | $\nu_{\text {obs }}, \mathrm{cm}^{-1}$ | $\Delta{ }^{\text {b }}$ | Line | C | $\mathrm{n}^{a}$ | $v_{\text {obs }} \cdot \mathrm{cm}^{-1}$ | $\Delta^{b}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| P(59) | Fl | 3* | 1023.1605 | -16 | P(32) | F1 | 2 | 1027.008 | 1 | Q (23) | Fl | 1* | 1031.163 | 5 |
|  | Al | 0* | . 2175 | -9 |  | F2 | $?$ | . 0105 | 2 | Q(22) | A2 | 1* | .1015 | 2 |
| P (58) | A1 | 3* | . 2105 | -12 |  | 入2 | 0 | . 0145 | -3 |  | F1 | 4* | . 149 | 4 |
|  | Fl | 10* | . 258 | -4 |  | $F 2$ | 3 | . 021 | 3 |  | Al | 1* | . 1855 | 4 |
| P(57) | Fl | 10 | . 1645 | -10 | P(30) | A1 | 1 | . 3095 | -8 | Q(20) | Al | 1* | .1545 | 10 |
|  | F2 | 9 | .172 | -11 |  | F1 | 3 | . 317 | -2 |  |  |  |  |  |
|  | Fl | 9 | . 1855 | -4 |  | F2 | 3 | - 319 | -1 | R(5) | F1 | ${ }^{1}$ | 1032.153 .155 | 6 -1 |
|  | E | 5 | . 196 | -10 |  | A2 | 1* | . 3335 | 3 |  | F1 | 0 | .155 .155 | -1 |
|  | A2 | 2 | . 2035 | -4 |  | F1 | 4* | . 3535 | -8 | R(7) | F2 | $\begin{aligned} & 0 \\ & 0 \end{aligned}$ | . .4025 | 6 7 |
|  | F1 | 8 | . 2225 | -9 |  | A 1 | 2* | . 3785 | -8 | $\mathrm{R}(7)$ $\mathrm{R}(8)$ | F1 | O* | . 524 | 5 |
|  | Al | 2* | . 250 | 2 | P(28) | A2 | 1** | . 654 | -7 |  | A1 | 0 * | . 534 | 2 |
| P (56) | Fl | 2* | 1024.2655 | 2 |  | Fl | 5* | 1029.6815 | -3 | R(11) | E | 1* | . 886 | 3 |
| P (54) | Al | 4** | 1024.0005 | 2 | P(15) | F1 | 2* | 1029.4145 | 0 | R(11) | Fl | 1 | . 8895 | -1 |
|  | F1 | 12* | . 0595 | 6 |  | A2 | 0* | . 433 | 7 |  | A2 | 0* | . 894 | -1 |
|  | A2 | 4* | 1023.123 | 13 |  | Fl | 0** | . 4485 | 7 -7 |  | F1 | 0 * | . 9015 | -2 |
| $P(53)$ | A1 | 1** | 1023.997 1024.0915 | 0 | P(13) | E | 1* | .680 .686 | -7 -2 | R(14) | E | 0* | 1033.2435 | 3 |
| P(52) | F1 | 7* | 1024.0915 .0705 | 6 |  | F2 | 1 | . 6888 | -4 |  | F2 | 1 ${ }_{0}$ | . 2485 | 0 |
|  | A2 | 2* | . 1055 | 7 |  | F1 | 2 | . 6895 | -4 |  | A2 | $0^{0}{ }^{\text {* }}$ | .271 .478 | -4 |
|  | Fl | 11* | . 3425 | -9 |  | AI | 0* | . 697 | 1 | R(16) | A1 | 0 | . $48485^{\circ}$ | -2 |
|  | Al | 4* | .405 | 12 |  | Fl | 0* | . 7105 | -4 |  | A1 | 1 | . $48459^{\circ}$ | 4 |
| P (51) | E | $6^{*}$ | . 080 | 5 | Q(53) | E | $8 *$ | 1030.756 | 7 |  | F2 | 1 | . $4872^{\circ}$ | 4 |
|  | Al | 2* | .115 .333 | 8 | Q(52) | FI | 7* | + 364 | -13 |  | A2 | 0 | $.4915^{\text {c }}$ | 4 |
|  | Fl | 3** | .333 .380 | 0 5 | Q(51) | Al | 1* | . 4125 | -1 |  | F2 | 2 * | .493 | 5 |
|  | Fl | 1* | . 431 | 7 |  | E | 7* | . 7245 | -2 |  | Fl | 2* | . 502 | -1 |
| P (50) | Fl | 6* | . 369 | 9 | Q(49) | Al | 1* | . 3795 | 2 |  | Al | 1** | . 517 | 5 |
|  | Fl | 8* | . 4385 | 12 |  | Fl | 5* | . 4455 | 0 | R (32) | Al | 2* | 1035.438 | 6 |
| P(49) | E | 7* | . 319 | -7 | Q(48) | Al Fl | 3** | . 354 | -6 | R(33) | F1 | 6 | . 3985 | -2 |
|  | Al | 3* | . 364 | 6 | Q (47) | A2 | 1* | . 4755 | 10 |  | F2 | 4 | . 412 | -3 -2 |
|  | Fl | 9 | . 428 | 11 | Q(46) | F2 | 2 | . 785 | 5 |  | Fl | 5 | . 414 |  |
|  | F2 | 8 | . 4325 | 11 | Q(45) | A 2 | 0* | . 424 | -1 |  | Fl | 3* |  | -3 |
|  | A2 | 2 | . 4465 | 20 | Q(45) | A1 |  | .724 .752 | -4 |  |  | 0* | . 4625 | 2 |
|  | F2 | 7 | . 451 | 16 |  | A1 | $2 *$ | .752 .3905 | -4 |  | A2 | $0 *$ 0 | . $46368{ }^{\text {c }}$ | 0 -5 |
|  | Fl | 8 | . 455 | 18 | $2(44)$ | A2 | 8* | .3905 .473 | 6 | R (34) | E2 | 0 | . $46887^{\circ}$ | -5 |
| P (45) | A2 | 3* | 1025.2435 | -9 |  | F1 | 4 | .473 .766 | -3 |  | El | 0 | . $46887^{\circ}$ | -6 |
|  | A2 | 0* | r +340 +332 | -2 | Q (43) | A2 | 0* | . 766 | -3 | R(35) | F1 | ${ }_{0}^{0}$ | .4687 .789 | -6 |
|  | Al | 0* | 332 .312 | 5 | Q(13) | Fl | 1* | . 440 | 7 | $\mathrm{R}(36)$ | Al | 2* | . 778 | -3 |
| P (43) | Fl | 6* | .312 .277 | 5 -1 |  | A 1 | 1 | . 7465 | -7 | R(45) | Al | 0* | 1036.891 | 4 |
|  | A | 2* | . 315 | -1 | Q(41) | A1 | 0* | . 4495 | 4 | R (46) | Fl | 8* | .9135 | -2 |
| P(42) | Fl | 7* | . 667 | -3 |  | Al | 1* | . 7295 | -8 | R (47) | Al | 1* | . 900 | -5 |
|  | AI | 3* | . 707 | -1 | $Q(40)$ | A1 | 3** | . 404 | 6 |  | F1 | 4* | . 9255 | 7 |
| P (41) | F1 | 7 | . 6705 | -5 |  | F1 | 5* | . 768 | -5 | R (48) | E | 0** | .894 | -1 |
|  | E | 4 | . 673 | 1 | $Q(39)$ | F1 | 3** | .7535 .7925 | -8 |  | E | 1** | 1037.921 | - |
|  | F2 | 6 | . 6795 | 2 | Q (37) | A2 | - * | . 7925 | -1 |  | A1 | 1** | 1037.283 | -5 |
|  | Fl | 6 | . 686 | 2 | Q (37) <br> (36) | A2 | 2** | .774 .7485 | -1 -14 | R (49) | F2 | 1* | . 286 | -3 |
|  | F2 | 5 | . 6995 | 3 | Q(36) | A2 | 0* | 1031.090 | -14 | R(50) | F1 | 2* | . 271 | -6 |
|  | A2 | 1 | . 7015 | 3 | O(35) | F1 | 1* | 1030.7895 | 3 | R(51) | A2 F1 | ${ }^{2 *}$ | - 308 | - ${ }^{2}$ |
|  | F1 | 5* | . 720 | -3 |  |  | 7* |  | -5 | R(51) | ${ }_{\mathrm{E}}$ | 8 |  | -5 -9 |
| P(40) | F1 | 7* | . 9495 | -14 | Q(34) | F1 | 2 | 1031.032 | -5 |  | E F 2 | 5 8 | .246 .253 | -9 |
|  | F1 | $8 *$ | 1026.0295 | -4 | Q (33) | F1 | 0* | 1030.7225 | -12 |  | F1 | 7 | . 2585 | -6 |
| P(39) | A 2 | 2 | 1025.9725 | -9 | Q(3) | A1 | 0 * | 1030.7995 | -12 |  | A2 | 2 | . 274 | 0 |
|  | F2 | 6 | . 976 | -9 |  | Fl | 6 |  |  |  |  |  |  |  |
|  | F1 | 6 | . 979 | -10 |  | F1 | 2* | 1031.0605 | -3 |  | F1 | 5** | . 2925 | 1 |
|  | Fl | 5 | . 992 | -6 |  | A1 | 2* | 1030.1365 | 4 |  | ${ }^{\text {A }}$ | 3* | - 3165 | 5 |
|  | A 2 | 1* | 1026.0335 | -1 | $Q(32)$ | A1 | 2* | 1030.764 | -4 |  | F1 | 3* | . 4145 | 0 |
|  | F1 | 3* | . 0615 | 8 |  | ${ }_{\text {A } 2}$ | 0 | 1031.0635 | $-3$ | R (52) | A1 | 0** | . 269 | -6 |
| P(38) | E | 0* | . 0555 | 4 | Q (31) | $E$ | 3 | . 094 | 5 |  | $E$ | 8** | . 2995 | 3 |
|  | Fl | 8* | . 3065 | - 12 | $Q$ (30) | F1 | 3 | . 0835 | 2 |  | E1 | 8* | . 4825 c | 2 |
|  | A 2 | 2* | . 351 | -5 | Q (29) | A2 | 1* | . 1325 | 0 | $R(53)$ | El | 9 | . 4341 | 2 |
| P(37) | A 2 | 1 | . 2875 | -7 | Q(28) | A2 | $1 *$ | . 1035 | 3 5 |  | E F 2 | 5 | .4385 .441 | 3 |
|  | F2 | 4 | . 299 | -5 |  | ${ }_{E}^{\text {A1 }}$ | 1 | . 1435 | -1 |  | F2 | 7 | . 445 | 8 |
|  | $F 1$ | 5 | . 3005 | -6 |  | $\stackrel{\rightharpoonup}{\mathrm{F}} 2$ | 1 | . 168 | $\frac{1}{7}$ |  | F1 | 6* | . 496 | 5 |
|  | A1 | 1* | . 320 | -1 | Q(27) | A1 | 0* | . .0985 | -3 | R (54) | ${ }_{E}$ | 0 * | . 453 | -1 |
|  | FI | 3* | . 345 | -3 | Q(27) | F2 | 3 | . 130 | -2 |  | E | 1* | . 4845 | 4 |
|  | A 2 | 0* | . 3745 | 0 |  | $\stackrel{-1}{ }$ | 5 | -184 | -4 |  | A1 | 3* |  | 1 |
| P(36) | A1 | 0* | . 3615 | 3 | Q(26) | A1 | 1* | . 18865 | - 3 | R(55) | A1 | 3 | . 6195 | 1 |
|  | E | O* | . 3915 | 5 | 0 (26) | F2 | 1 | . 1985 | 9 | R(55) | A1 | 2 | . 619. | -1 |
| P (33) | Al | O* | . 9975 | -2 |  | A1 | \%* | . 1068 | -5 |  | F1 | 8 | . .638 |  |
| P(32) | E | 1* | . 9905 | -1 | O(24) | A12 | 1* | . 1385 | -2 |  | ${ }_{\mathrm{E}}$ | 5 | . 6385 | 5 |
|  | A1 | 0 | 1027.006 | 1 |  | A1 | 1 | -1905 | -5 | R (56) | E | 1* | . 634 | 2 |

[^1]TABLE II
$\nu_{3}$ Spectroscopic Constants of ${ }^{28} \mathrm{SiF}_{4}{ }^{\text {a }}$

| Scalar constants: | Tensor constants: |
| :---: | :---: |
| $m=1031.39661(13)$ | $\mathrm{g}=4.1771(23) \times 10^{-5}$ |
| $\mathrm{n}=0.127726(4)$ | $h=3.15(5) \times 10^{-8}$ |
| $(\mathrm{B} \mathrm{\zeta})_{3}=0.0743(4)^{b}$ | $k=1.28(13) \times 10^{-10}$ |
| $p=-2.5489(20) \times 10^{-4}$ | $\mathrm{u}=\mathrm{z}^{\prime}=0$ |
| $v=-3.787(3) \times 10^{-4}$ | Derived constants: |
| $\mathrm{q}=-1.36(18) \times 10^{-8}$ | $\mathrm{Z}_{3 s} \approx \mathrm{v}-\mathrm{p}$ |
| $s=-1.10(6) \times 10^{-9}$ | $=-1.238(3) \times 10^{-4}$ |
| $w=2.0(11) \times 10^{-10}$ | $Y_{3} \approx(v+2 p) / 3$ |
|  | $=-2.962(2) \times 10^{-4}$ |

${ }^{a}$ In $\mathrm{cm}^{-1}$; standard deviations, in parentheses, given in units of the last decimal place quoted.
${ }^{b}$ Fixed; see text.
that of $B_{3}$. This error in $B_{3}$ is also of the same magnitude as higher-order corrections to Eq. (4b). As described above, we were able to fit $B \zeta_{3}$ as a free parameter. We obtained the value

$$
\begin{equation*}
B \zeta_{3}=0.0777(16) \tag{6}
\end{equation*}
$$

which is less accurately determined than the value obtained from electron diffraction, but in reasonable agreement.

Using the 10 spectroscopic constants in Table II, we have calculated all the ${ }^{28} \mathrm{SiF}_{4}$ $\nu_{3}$ transition frequencies for $J^{\prime} \leq 70$. A listing can be provided upon request. In Table I we compare the calculated frequencies with their measured values. The overall standard deviation is $6 \times 10^{-4} \mathrm{~cm}^{-1}$ which should be compared with the Doppler width (FWHM) of $1 \times 10^{-3} \mathrm{~cm}^{-1}$ at 200 K .

Because of the accuracy of our calculated frequencies, it is now possible to assign unambiguously the $\mathrm{SiF}_{4}$ transitions seen in the ${ }^{12} \mathrm{C}^{16} \mathrm{O}_{2}$ saturation spectra. Indeed, eight lines from the data mentioned above near the $\mathrm{CO}_{2} P(30), P(32)$, and $P(34)$ lines were assigned to $R(53), R(34)$, and $R(16)$ transitions, respectively. These eight lines are also listed in Table I and were included in our fit. All other transitions of ${ }^{28} \mathrm{SiF}_{4}$ from the vibrational ground state within $\pm 200 \mathrm{MHz}$ of $\mathrm{CO}_{2}$ laser lines between 1023 and $1038 \mathrm{~cm}^{-1}$ are listed in another publication (12). From Table I one finds that the triplet reported by Harter et al. (2) near the $\mathrm{CO}_{2} P(32)$ line
is an $R(34) F_{2}^{0}+E^{0}+F_{1}^{0}$ cluster. They also report an $A_{1}+F_{1}+F_{2}+A_{2}$ cluster nearby which belongs to an unassigned hot band.

Our calculations indicate the $P(36)$ line of $\mathrm{CO}_{2}$ is between the $Q(1)$ and $R(0)$ lines of ${ }^{28} \mathrm{SiF}_{4}$, detuned by 2.43 and 1.41 GHz , respectively. Thus multiple-photon absorption by ${ }^{28} \mathrm{SiF}_{4}$ when pumped by the $P(36) \mathrm{CO}_{2}$ line can only originate from vibrational hot bands or multiphoton resonances to $2 \nu_{3}$ or $3 \nu_{3}$ disregarding power broadening effects. In the photon echo experiments with $\mathrm{SiF}_{4}$, Gutman and Heer (5) correctly infer high- $J R$-branch absorption when pumping with $9.4-\mu \mathrm{m} P(30)$ to $P(34)$ lines of $\mathrm{CO}_{2}$. Their lack of signal for $P(28)$ pumping is probably a result of the small rotational population for $J>70$ giving rise to weak $R$-branch transitions. In the two-frequency experiments of Akulin et al. (9,10), the $P(38) 9.4-$ $\mu \mathrm{m} \mathrm{CO}_{2}$ line was successfully used to pump $\mathrm{SiF}_{4}$ near $P(15)$.

We hope that with the identifications made in the saturation spectra of $\nu_{3}$ of $\mathrm{SiF}_{4}$ a comprehensive effort to resolve the hyperfine structure can be undertaken similar to that achieved for $\mathrm{SF}_{6}(29,30)$. We note that in $T_{d}$ symmetry with nuclear spin $1 / 2$ the species of $F_{1}^{+}, F_{2} A_{1}^{-}, A_{2}^{+}, E^{ \pm}$have distinct inversion character ( + or -) and crossover resonances cannot arise from hyperfine mixing of species with different inversion character (31).

## $\nu_{3}$ TRANSITION DIPOLE MOMENT

From band strength measurements (32), the $\nu_{3}$ transition dipole moment of $\mathrm{SiF}_{4}$ has been calculated (33) to be $\left|\mu_{3}\right|=0.276(14) D$. This dipole moment can also be determined from individual rovibrational line strengths according to the formula (33)

$$
\begin{equation*}
S_{i f}=\frac{8 \pi^{3} N}{3 h c Z} \nu_{i f} \mu_{3}^{2} \epsilon_{i}\left(2 J^{\prime}+1\right) e^{-B_{0} h c /(J+1) / k T}\left(1-e^{-h c \nu_{i f} / k T}\right) . \tag{7}
\end{equation*}
$$

Here $N$ is the number of molecules per $\mathrm{cm}^{3}, Z=Z_{V} Z_{R}$ is the product of the vibrational and rotational partition functions, and $\nu_{i f}$ is the wavenumber of the transition. The units in this equation are $\mathrm{cm}^{-2}$ where $\mu_{3}$ is in esu-cm ( $1 D=1$ $\times 10^{-18}$ esu-cm). The nuclear-spin statistical weight is $\epsilon_{i}=5,2$, and 3 for species $A, E$, and $F$ respectively. The rotational partition function is approximately (34)

$$
\begin{equation*}
Z_{r}=\frac{4}{3} \pi^{1 / 2}\left(\frac{B_{0} h c}{k T}\right)^{-3 / 2} e^{B_{0} h c / 4 k T} . \tag{8}
\end{equation*}
$$

If the linewidth $\gamma$ (FWHM) is Doppler-limited, we may relate the line strength to the peak height $k_{i f}$ by the standard relation

$$
\begin{equation*}
S_{i f}=k_{i f} \gamma_{D}\left(\frac{\pi}{4 \ln 2}\right)^{1 / 2} . \tag{9}
\end{equation*}
$$

We have measured the peak heights of various rovibrational transitions in the $R$ branch, where the diode was operating with sub-Doppler resolution. Peak height measurements were made in a pressure range of 0.7 to 20 Pa to minimize the pressure broadening. In this range the measured linewidths were always Dopplerlimited which is consistent with the 19 nsec-Torr dephasing time ( $T_{2}$ ) as measured

TABLE III
Dipole Transition Moments for Selected Rovibrational Lines of $\nu_{3}$ of ${ }^{28} \mathrm{SiF}_{4}$

| Line | T, K | Pressure, Pa | $\nu_{i f}, \mathrm{~cm}^{-1}$ | $\left\|\mu_{3}\right\|$, Debye |
| :---: | :---: | :---: | :---: | :---: |
| $R(18) \mathrm{F}_{1}^{1}$ | 296 | $0.7-4.0$ | 1033.722 | 0.292 |
| $R(19) A_{1}^{0}$ | 296 | $0.7-4.0$ | 1033.839 | 0.308 |
| $R(20) \mathrm{F}_{2}^{1}$ | 296 | $0.7-20.0$ | 1033.949 | 0.286 |
| $R(20) A_{1}^{0}$ | 296 | $3.3-20.0$ | 1033.955 | 0.327 |

by Gutman and Heer (5). The minimum pressure used was limited by the signal detection.

The peak heights were measured for at least three different pressures and the dipoles given for each line represent an average. As shown in Table III the calculated transition dipoles for the four lines measured are close to that calculated from the $\nu_{3}$ band strength. The error in our $\left|\mu_{3}\right|$ is of the order of $10 \%$, so the discrepancies between the $\left|\mu_{3}\right|$ of various lines may not be significant. Any hot band absorption, which should be prevalent in the room temperature measurements, would result in a value for $\left|\mu_{3}\right|$ too large. Our values for $\left|\mu_{3}\right|$ are consistently higher than the dipole moment reported previously but this value is within our experimental error. Our higher values confirm that the resolution of our instrument was indeed sub-Doppler.

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[^1]:    An asterisk indicatas that the transition shown is a member of a tight, unresolved ciuster
    $b$ of several transitions $_{\Delta}=\left(v_{\text {obs }}-\mathrm{cm}^{-2}\right.$.
    Frequency from saturation spectrum.

